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Exploration of Oxyfluoride Frameworks as Na-ion Cathodes

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practical utilization of NIBs in applications, it is important to boost the energy and power densities of the electrodes being used by the discovery of novel candidate materials. Thus, we explore the chemical space of transition metal-containing oxyfluorides (TMOFs) that adopt a perovskite structure as possible NIB electrodes. Our choice of the perovskite structure is motivated by the "large" cationic tunnels that can accommodate Na⁺, while the

Roadmap to find potential oxyfluorides as Na-ion battery cathode

chemistry of TMOFs is motivated by the high electronegativity and inductive effect of F[−], which can possibly lead to higher voltages. We use density functional theory-based calculations to estimate the ground state polymorphs, average Na (de)intercalation voltages, thermodynamic stabilities, and Na⁺ mobility on two distinct sets of compositions: the F-rich Na_{*x*}MOF₂ and the O-rich Na_{1+*x*}MO₂F, where *x* = 0−1 and M = Ti, V, Cr, Mn, Fe, Co, or Ni. Upon identifying the ground state polymorphs in the charged compositions (i.e., MOF_2 and $NAMO_2F$), we show that F-rich perovskites exhibit higher average voltages compared to those of the O-rich perovskites. Also, we find six stable/metastable perovskites in the F-rich space, while all the O-rich perovskites (except NaTiO₂F) are unstable. Finally, our Na-ion mobility calculations indicate that TiOF₂−NaTiOF₂, VOF₂−NaVOF₂, CrOF₂, and NaMnOF₂ can be promising compositions, albeit with challenges to be resolved, for experimental exploration as NIB cathodes. These oxyfluoride compositions can be promising if used primarily in a strained electrode configuration and/or in thin film batteries. Our computational approach and findings provide insights into developing practical NIBs involving fluorine-containing intercalation frameworks.

■ **INTRODUCTION**

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Na-ion battery (NIB) technology is a key contributor in reducing the extensive dependence on Li-ion batteries (LIBs) to fulfill the ever-increasing energy demands. $1-5$ $1-5$ $1-5$ As a technology, NIBs have come a long way with notable applications in both electric vehicles and stationary energy storage. $6-9$ $6-9$ $6-9$ Nevertheless, the practical utility of NIBs can be further enhanced with the development of novel high energy and power density electrode materials. While layered transition-metal oxides (TMOs) are the state-of-the-art NIB positive electrodes (cathodes), 10 10 10 the structural instabilities of layered compounds at their fully desodiated states and detrimental phase transitions have directed research toward polyanionic cathode frameworks.[11](#page-10-0)−[13](#page-10-0) Some of the most explored polyanionic frameworks, such as sodium superionic conductors (NaSICONs), alluaudites, olivines, and pyro/ fluoro-phosphates, display a wide range of electrochemical performance and good structural stability, with low gravimetric capacity being a common impediment.^{[12](#page-10-0)} Thus, an ideal NIB cathode must be able to (de)intercalate the large $Na⁺$ at high rates, without compromising structural stability, and deliver a

large capacity for achieving both high energy and power densities. An ideal NIB negative electrode (anode) also has similar requirements as the ideal cathode.

Oxide perovskites, which have a general formula of ABO_3 , where A and B are cations, have been explored for several applications beyond energy-storage, due to their structural stability and compositional flexibility.^{[14](#page-10-0)−[18](#page-10-0)} Importantly, perovskites are suitable structures for accommodating Na⁺ because of their rigid open structures with large voids.^{[19](#page-10-0)} Additionally, the incorporation of fluorides in cathode frameworks often leads to improved energy densities, since the higher electronegativity of F[−] typically leads to a higher (de)intercalation voltage via the induction effect.^{20−[22](#page-10-0)} Indeed, many of the best-performing polyanionic NIB cathodes contain fluorine.^{23-[25](#page-10-0)}

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Figure 1. Workflow to obtain the ground state polymorph for desodiated F-rich MOF₂ and O-rich NaMO₂F perovskites, where M = Ti, V, Cr, Mn, Fe, Co, or Ni. Notations "pmg" and "ICSD" refer to the pymatgen package and the inorganic crystal structure database.

Thus, fixing the A cation in a perovskite as Na⁺, the B cation to be a redox-active 3*d* transition metal (TM), and the anions being a mixture of both O and F yields a class of perovskitebased TM oxyfluoride (TMOF) compositions as potential NIB cathodes (or anodes).

So far, perovskite TMOFs are a largely unexplored class of battery cathodes (or anodes), primarily due to synthesis difficulties from highly stable fluoride precursors.²⁶ Indeed, only a few TMOFs, including, TiOF₂ (space group: $Pm\overline{3}m$),²⁷ VO₂F $(R\overline{3}c)$,^{[28](#page-10-0),[29](#page-10-0)} and NbO₂F $(Pm\overline{3}m)$,^{[27](#page-10-0)} have been investigated as LIB cathodes. Additionally, $Li₂MO₂F$ with M across the 3*d* series³⁰ and $\text{Na}_2\text{MnO}_2\text{F}^{31}$ $\text{Na}_2\text{MnO}_2\text{F}^{31}$ $\text{Na}_2\text{MnO}_2\text{F}^{31}$ have been reported to exhibit a disordered rocksalt and not a perovskite-based structure. Also, most of the oxyfluoride structures that have been reported have undergone either amorphization or an irreversible structural transition during electrochemical cycling.[32](#page-10-0)[−][35](#page-10-0) Although Li-ion mobility is not hindered in both disordered rocksalt^{[36](#page-10-0)} and amorphized^{[37](#page-10-0)} oxyfluorides, studies have not analyzed Na-ion mobility in similar frameworks. Notably, the rutile-FeOF (*P*4₂/*mnm*) structure was tested as a NIB cathode and showed a reversible transition to cubic- $Na_xFeOF.³⁵$ However, this FeOF \leftrightarrow Na_xFeOF transition was accompanied by significant hysteresis in the corresponding voltage−capacity profiles, with possible contributions from electrolyte decomposition and/or other side reactions.^{[35](#page-10-0)} Importantly, the chemical class of TMOFs has not been systematically explored, either computationally or experimentally, as NIB cathodes, so far.

Here, we present a systematic density functional theory (DFT)-based computational exploration of perovskite-based TMOF compositions as potential NIB cathodes (or anodes). Specifically, we explore the chemical compositions of oxygenrich (NaMO₂F \leftrightarrow Na₂MO₂F) and fluorine-rich (MOF₂ \leftrightarrow NaMOF₂) perovskites, where $M = Ti$, V, Cr, Mn, Fe, Co, or Ni. For both the O-rich and F-rich compositions, we examine possible crystalline structures of the general perovskite framework. Importantly, we have evaluated the ground state Na-vacancy configurations, average Na intercalation voltages, and 0 K thermodynamic stabilities in both O-rich and F-rich TMOFs, followed by an evaluation of the Na-ion mobility in a subset of candidate compounds. Besides shedding light on the overall trends in voltages and stabilities, we also identify a few promising compositions, namely, TiOF₂−NaTiOF₂, VOF₂− $NaVOF₂$, $CrOF₂$, and $NaMnOF₂$, as candidate NIB electrodes, which can be relevant for subsequent experimental validation, primarily in strained configurations. We hope that our study opens up the novel oxyfluoride chemical space for battery cathode applications and beyond.

■ **METHODS AND WORKFLOW**

Structure Identification. To explore the TMOF chemical space, we used the charged-O (i.e., NaMO_2F) and F-rich $(MOF₂)$ compositions as the initial cases of the structure generation for all TMs. Note that both charged compositions correspond to the TM being in a +4 oxidation state, while the corresponding discharged compositions $(Na_2MO_2F$ and NaMOF₂) reflect the TM in a +3 oxidation state. To identify

Figure 2. (a) NaTiO₂F with the initial Na atom (denoted by Na1) at the center of the cube (i.e., fractional coordinates of $(0.5, 0.5, 0.5)$). (b) Displacement of the Na1 atom to (0.25, 0.25, 0.25) and the subsequent occupation of the second Na atom (denoted by Na2) at (0.75, 0.75, 0.75). Blue polyhedra in both panels denote TiO₄F₂ octahedra. O and F are represented by red and purple spheres, respectively. Body diagonals within the cubic structures are indicated by dotted black lines.

the relevant space group/polymorph, we first searched the inorganic crystal structure database $(ICSD)^{38}$ $(ICSD)^{38}$ $(ICSD)^{38}$ for experimental structures with the NaMO₂F and MOF₂ compositions, where we found only TiOF₂ (ICSD collection code 160661; *Pm3m*), VO₂F (ICSD collection code 142594; $R\overline{3}c$), and LiVO₂F (ICSD collection code 142596; *R3*̅*c*). Thus, we used the TiOF₂ structure from the ICSD as the starting configuration for all calculations involving cubic-TiOF₂, VO₂F for calculations of rhombohedral-MOF₂, and LiVO₂F for calculations of rhombohedral-NaMO₂F.

Given the absence of ICSD structures for other TMOFs, we theoretically generated possible structures for both charged compositions using the workflow displayed in [Figure](#page-1-0) 1. Similar to the procedure used in a previous study, 18 we used experimental template structures among six different space groups that are commonly adopted by perovskite compositions to generate six possible theoretical structures for each composition. Specifically, we used $CaTiO₃$, BaTiO₃, NaN bO_2F , BaRhO₃, LiVO₂F, and CeVO₃ as templates for the *Pm3*̅*m*, *P*4*mm*, *Pbnm*, *P*63/*mmc*, *R3*̅*c*, and *P*2/*b* space groups, respectively. Note that we did not consider any ReO_3 -type^{[19](#page-10-0)} (or perovskite-type) hydroxides, Prussian blue analogs, or formate compositions as templates largely due to the presence of water molecules and/or incompatibilities in the size of Acation required in such structures.

We chose Ba and Ca containing structures as templates due to the similarity in the ionic radii of Ba^{2+} and Ca^{2+} to Na^{+} . Although $CaTiO₃$ is known to be an orthorhombic perov-skite,^{[39](#page-10-0)} we used CaTiO₃ as a template for the cubic perovskite owing to the similarity in the ionic radii of Na^+ and \bar{Ca}^{2+40} \bar{Ca}^{2+40} \bar{Ca}^{2+40} and the availability of the Ca-containing perovskite structure 41 in the ICSD. $CeVO₃$ was the only reasonable monoclinically distorted perovskite template we could find. For rhombohedral perovskites, the presence of $VO₂F$ and $LIVO₂F$ experimental structures provided us both an oxyfluoride template along with possible Na sites, as Li can be substituted with Na,^{[42](#page-10-0)} motivating our use of $LiVO₂F$ as the template.²⁸ As far as the orthorhombic perovskite, $NaNbO₂F$ is an oxyfluoride and contains Na, and hence, it was the obvious choice as a template. Note that we used the TiOF₂ structure as the *Pm3m*

template for NaMO_2 F compositions. In addition, we used the $VO₂F$ structure as the $R\overline{3}c$ template for all rhombohedral- MOF_2 compositions and the LiVO₂F structure as the *R3*^{*c*} template for all rhombohedral-NaMO₂F compositions.

From each template structure, we performed chemical substitution (i.e., replace Ca/Ba/Li/Ce with Na and the remaining cation with a $3d$ TM), to result in a $NaMO_3$ composition. Subsequenty, we used the RLSVolumePredic- $tor⁴³$ $tor⁴³$ $tor⁴³$ class of the pymatgen package to scale the lattice parameters of the template structure to values that better represent a $NaMO₃$ perovskite composition. Upon lattice scaling, we introduced F, based on an O:F ratio of 2:1 in Orich perovskites and 1:2 in F-rich perovskites, by inducing disorder within the anionic sublattice using the Substitution-Transformation class of pymatgen. Note that in F-rich perovskites, we removed Na before the lattice scaling step. Finally, we enumerated symmetrically distinct O−F arrangements for all distinct template space groups in both the $NaMO₂F$ and $MOF₂$ compositions, using the OrderDisorderedStructureTransformation class of pymatgen, and performed DFT calculations to determine the respective ground state configurations. During enumerations, we took a maximum of 16 structures that exhibited the lowest electrostatic energy, calculated using the Ewald summation technique, 44 to minimize computational expense. In the case of *P4mm* and $R\overline{3}$ *c* perovskites (both $MOF₂$ and $NaMOF₂$), we obtained a total of only five and three symmetrically distinct configurations upon enumeration and all configurations were considered for DFT calculations. In the case of *Pm3m*, *Pbnm*, *P*63/*mmc*, and *P*2/*b* space groups, we obtained a total of 22, 40, 55, and 48 symmetrically distinct configurations, respectively, out of which we chose the 16 lowest electrostatic energy configurations for each space group (for both $MOF₂$ and $NaMOF₂$).

Once the ground state polymorph of each desodiated NaMO_2 F and MOF_2 composition was determined, we added Na to the DFT-relaxed charged ground state structures to obtain the corresponding discharged (or sodiated) configurations, i.e., $Na₂MO₂F$ and $NaMOF₂$. For $NaMOF₂$, we initialized the Na ions on the sites occupied by the A-cation in

the corresponding template perovskite structure. Given that the NaMOF₂ perovskite only has one distinct Na (or A cation) site, we created a second Na site by displacing the existing Na ion to minimize electrostatic repulsion between the two Na ions, as displayed in [Figure](#page-2-0) 2. For example, in the case of *Pm3m* NaTiO₂F, we displaced the existing Na from the center of the cube (i.e., fractional coordinates of (0.5, 0.5, 0.5)) along the body diagonal to a new site of coordinates (0.25, 0.25, 0.25). Subsequently, we initialized the second Na atom at the coordinates of (0.75, 0.75, 0.75), to minimize electrostatic repulsions between the two Na. The introduction of additional Na sites in other perovskite structures is described in the Supporting [Information](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf), along with a schematic in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S1.

Computational Details. We used the Vienna ab initio simulation package (VASP)^{[45,46](#page-11-0)} for all spin-polarized DFT calculations. We utilized the projector augmented-wave $(PAW)^{47,48}$ $(PAW)^{47,48}$ $(PAW)^{47,48}$ $(PAW)^{47,48}$ $(PAW)^{47,48}$ potentials similar to our previous work,^{49-[51](#page-11-0)} with the list of PAW potentials used in this work compiled in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S1. To account for the electronic exchange and correlation, we employed the Hubbard *U* corrected,^{[52,53](#page-11-0)} strongly constrained and appropriately normed (i.e., SCAN +*U*) [49,50,54](#page-11-0) functional. We utilized *U* values that were obtained for TMOs in our work,^{[49](#page-11-0),[50](#page-11-0)} since they gave the best agreement between the calculated and experimental average voltages in Li-based TMOFs (see [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S2). We expanded the oneelectron wave functions using a plane wave basis set, with a 520 eV kinetic energy cutoff, and used a Gaussian smearing of width 0.05 eV to integrate the Fermi surface. We sampled the irreducible Brillouin zone with a Γ -centered Monkhorst-pack⁵⁵ *k*-mesh with a density of at least 32 *k*-points per Å (i.e., a minimum sampling of 32 subdivisions along each unit reciprocal lattice vector). For the total energies and atomic forces, we set the convergence criterion to be 0.01 meV and | 0.03 | eV/Å, respectively. To reduce computational complexity, we initialized all 3*d* TMs in their corresponding high-spin ferromagnetic configurations. For all structures, we relaxed the cell volume, cell shape, and ionic positions without preserving any symmetry. Where possible, we have followed a color-blind friendly color scheme in our plots.^{[56](#page-11-0)}

Tolerance Factors. We calculated the Goldschmidt tolerance factor $(t)^{57}$ $(t)^{57}$ $(t)^{57}$ using eq 1 for Na-TMOFs, which adhere to the ABO₃-type stoichiometry.^{[57](#page-11-0)} Compositions with cornershared octahedra (i.e., *Pm3*̅*m*, *P*4*mm*, *Pbnm*, and *P*2*/b* space groups) and with $0.825 < t < 1.059$ are 74% likely to be accurately labeled as an ideal perovskite structure.^{[57](#page-11-0),[58](#page-11-0)} For compositions with isolated octahedra (i.e., *P*63*/mmc*, and *R3*̅*c*), *t* should ideally label the structures as nonperovskites. In eq 1, r_A represents the Shannon ionic radii of 12-coordinated Na⁺, while r_B signifies the Shannon radii of 6-coordinated TM^{3+} and TM⁴⁺ for sodiated and desodiated TMOF, respectively. r_X denotes the weighted Shannon radii of the of 6-coordinated anion, with the weights corresponding to the relative content of O and F in the TMOF.^{[59](#page-11-0)} For the Na₂MO₂F compositions, we used r_A of a single 12-coordinated Na⁺ and r_B to be 6coordinated TM^{3+} for the sake of comparison with other TMOF compositions considered, even though *t* is not actually developed for A_2BO_3 compositions. We also utilized eq 2 to calculate the tolerance factor (τ) developed by Bartel et al.,⁶⁰ which has a 92% accuracy rate in correctly labeling compositions with perovskite structures as a perovskite. *τ* takes into account the oxidation state of Na (denoted as n_A), apart from r_A , r_B , and r_X used for *t*, and considers a structure an ideal perovskite when τ < 4.18.^{[60](#page-11-0)} Note that both *t* and τ factors

cannot be applied to the $MOF₂$ stoichiometry due to the absence of the A-cation in the structure.

$$
t = \frac{r_{A} + r_{X}}{\sqrt{2}(r_{B} + r_{X})}
$$
\n⁽¹⁾

$$
\tau = \frac{r_{\rm X}}{r_{\rm B}} - n_{\rm A} \left(n_{\rm A} - \frac{r_{\rm A}/r_{\rm B}}{\ln(r_{\rm A}/r_{\rm B})} \right) \tag{2}
$$

Ab Initio Thermodynamics. For evaluating the thermodynamic stability of the TMOFs considered, we constructed the 0 K convex hull of the corresponding quaternary (i.e., Na− TM−O−F) chemical spaces by using the pymatgen package. Specifically, we collected experimentally reported structures of individual elements (Na, TM, O, and F), binaries (Na−O, Na−F, TM−O, and TM−F), ternaries (Na−O−F, TM−O−F, Na−TM−O, Na−TM−F), and quaternaries (Na−TM−O−F) from the ICSD and subsequently calculated their total energies using DFT. Note that we only considered ICSD structures that were fully ordered; i.e., each lattice site in a structure exhibits an integer occupation of a given species. Also, for individual elements, Na−O and Na−F binaries, and Na−O−F ternaries, we used only the SCAN functional for treating the electronic exchange and correlation, while for the other structures, we used the SCAN+*U* functional. Since we have utilized only DFT-calculated total energies to construct the 0 K convex hull, our phase diagrams do not include the *p*−*V* contributions.

Importantly, any stable entity on the 0 K convex hull will have a energy above convex hull (E^{hull}) as 0 meV/atom, while any metastable/unstable entity will have $E^{\text{hull}} > 0.61$ $E^{\text{hull}} > 0.61$ Given that compounds that are metastable at 0 K can be stabilized under different experimental conditions, we used a synthesizeability threshold of $E^{\text{hull}} \leq 100 \text{ meV/atom.}^{62}$ This implies that compounds with a $E^{\text{hull}} \leq 100 \text{ meV/atom may be synthesized}$ under higher temperatures/pressures and can be considered metastable, while compounds with *E*hull > 100 meV/atom are unlikely to be synthesized and can be considered to be unstable. All calculated phase diagrams (except for the Na− Ti−O−F quaternary) are compiled in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S4, while the list of stable/unstable compounds is compiled in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S5.

The average voltage for Na (de)intercalation in TMOFs is evaluated using DFT-based total energies from the well-known Nernst equation.^{[63](#page-11-0)} Considering a Na (de)intercalation reaction of the form, $\text{Na}_{x} \text{TMOF} + \Delta x \text{Na} \leftrightarrow \text{Na}_{x+\Delta} x \text{TMOF}$, we can approximate the Gibbs energy change (Δ*G*) associated with the (de)intercalation process using eq 3, which neglects entropic and *p*−*V* contributions. Note that the *E* terms in eq 3 are DFT-calculated, with Na*x*TMOF and Na*x*+Δ*x*TMOF described with SCAN+*U* and metallic Na described with SCAN in its body-centered-cubic ground state. *F* is Faraday's constant.

$$
\langle V \rangle = -\frac{\Delta G}{\Delta xF} \approx -\frac{E(Na_{x}TMOF) - [E(Na_{x}TMOF) + \Delta xE(Na))]}{\Delta xF}
$$
\n(3)

Kinetics. To estimate the ionic mobility of $Na⁺$ in the selected TMOF frameworks, we utilized a DFT-based nudged elastic band $(NEB)^{64,65}$ $(NEB)^{64,65}$ $(NEB)^{64,65}$ $(NEB)^{64,65}$ $(NEB)^{64,65}$ calculations to estimate the migration barrier (E_m) associated with Na⁺ motion. For all structures, we considered a vacancy-mediated $Na⁺$ migration along the A-site "tunnel" of the perovskite framework and calculated *E*^m either

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Figure 3. Percentage-normalized relative energies of all polymorphs considered with respect to the corresponding ground states for (a) F-rich MOF2 and (b) O-rich NaMO2F. All ground state polymorphs are indicated by colored solid arrows as per the color of the respective ground state polymorph. Each concentric ring on the radars represents a percentage step of 20%.

Figure 4. Calculated (a) Goldschmidt (t) and (b) Bartel et al. (τ) tolerance factors for NaMOF₂ (orange diamonds), NaMO₂F (dark blue circles), and Na2MO2F (light blue circles). Threshold values for perovskite formation, namely 0.825 < *t* < 1.059 and *τ* < 4.18 are indicated by the shaded gray and shaded pink regions in panels a and b, respectively.

at the charged or the discharged sodium concentration limits. Upon introducing a Na-vacancy and fully relaxing the end point configurations, we interpolated five images across the end points to initialize the minimum energy path (MEP).

A spring constant of 5 eV/\AA^2 was introduced between the images, and we considered the NEB calculation converged when the total energy of each image and the perpendicular component of the force between each image dropped below 0.01 meV and | 0.05 eV/Å, respectively. For all NEB | calculations, we used supercells with lattice parameters of \geq 8 Å to avoid spurious interactions of the migrating Na with its periodic images. We used the Perdew−Burke−Ernzerhof $(PBE)^{66}$ parametrization of the generalized gradient approximation (GGA) to describe the exchange-correlation in our NEB calculations instead of SCAN, since GGA provides accurate qualitative trends at lower computational cost and with fewer convergence difficulties. 67 We performed full structure relaxations of our initial and final images with GGA before performing the NEB. All computed MEPs are compiled in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S5, and the $Na⁺$ migration pathway in TiOF₂ is illustrated in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S6.

■ **RESULTS**

Ground State Polymorphs. The ground state polymorphs for each desodiated F-rich $MOF₂$ and O-rich NaMO2F are represented by the black arrows in panels *a* and *b* of Figure 3. The percentage normalized differences in energies of the other polymorphs considered, relative to the ground state, are plotted as bars in Figure 3. Specifically, we have plotted the percentage differences, calculated as $E(\text{polymorph}) - E(\text{ground state}) \times 100$
 $E(\text{highest–energy polymorph}) - E(\text{ground state}) \times 100$ $E(\text{polymorph}) - E(\text{ground state})$
(highest-energy polymorph) – $E(\text{ground state}) \times 100$, where each concen-

tric ring on the radars represent percentage steps of 20%. Thus, the ground state and the highest energy polymorph represent 0% and 100%, respectively, on the radar of Figure 3 for each composition. Notably, the ground state polymorphs of the MOF2 compositions include *Pbnm* (for Ti, V, Fe), *R3*̅*c* (Cr, Mn, Ni), and $P2/b$ (Co), while those of the NaMO₂F compositions are *P2/b* (Ti, V, Mn, Fe, Co), *Pbnm* (Cr), and *R* $3c$ (Ni). We have compiled the percentage normalized relative energies and the actual relative energies for all perovskite polymorphs considered in [Tables](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S3 and [S4](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf), respectively, and provided the schematics of the desodiated ground states and their corresponding sodiated structures in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S2.

Figure 4 displays the *t* and *τ* tolerance factors estimated for F-rich NaMOF₂ and for O-rich NaMO₂F and Na₂MO₂F, with their respective values tabulated in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S7. We have also compiled the *t* and *τ* values for Li-based perovskite TMOFs, with compositions of $LimOF_{2}$, $LiMO_{2}F$, and $Li_{2}MO_{2}F$ given in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S7 for comparison.

Notably, all the Na-TMOF stoichiometries lie within the range of $0.825 < t < 1.059$,^{[57](#page-11-0)} as shown in Figure 4a, indicating that *t* could correctly label compositions with ground state polymorphs as *Pbnm* (F-rich NaMOF₂ with M as Ti, V, and Fe, and O-rich NaMO_2 F and Na_2MO_2 F with M as Cr) and $P2/b$ (F-rich NaMOF₂ with M as Co and O-rich NaMO₂F and $Na₂MO₂F$ with M as Ti, V, Mn, Fe, and Co) as perovskites. However, *t* of compositions with rhombohedral or hexagonal perovskite structures should lie outside the range of 0.825 < *t* <

Figure 5. Calculated average Na (de)intercalation voltages (in V), versus Na/Na⁺, in F-rich (orange bars) and O-rich (blue bars) TMOFs considered.

Figure 6. Ternary projections of the Na–Ti–O–F phase diagram to visualize (a) TiOF₂, (b) NaTiOF₂, and (c) NaTiO₂F and Na₂TiO₂F. In each panel, the green-to-white background represents *E*^{formation}, while the red diamonds indicate meta/instability (*E*^{hull} > 0). Black circles indicate stable compositions and black lines are tie-lines.

1.059,^{[57](#page-11-0)} which implies that F-rich NaMOF₂ with M as Cr, Mn, and Ni, and O-rich NaMO_2F and Na_2MO_2F with M as Ni have been incorrectly classified. For Li-TMOF stoichiometries, all Li₂MOF₂, LiTiO₂F, and LiVO₂F have $t < 0.825$ ([Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S7), showing their possibility to form ilmenite structure⁵⁷ $(R3)$ which is in line with the observation of the rhombohedral structure maintained during the intercalation reaction of $VO₂F$ \leftrightarrow LiVO₂F.^{[28](#page-10-0),[29](#page-10-0)} However, *R*3*c* LiVO₂F irreversibly transitions to *Pm3m* Li₂VO₂F^{[28,29](#page-10-0)} upon lithiation which might contradict the labeling based on *t*.

In the case of calculated *τ* values [\(Figure](#page-4-0) 4b), we observe NaMO₂F with M = Ti, V, and Fe lie below the threshold τ = 4.18, but $M = Cr$, Mn, Co, and Ni lie above 4.18, which suggests that *τ* is categorizing NaCrO₂F, NaMnO₂F, and NaCoO2F perovskites with the *P2/b* ground state structure as a nonperovskite, in contrast to the labeling by *t*. Given that *τ* is a more accurate labeler of perovskite compositions than *t*, we expect some of the Na-containing O-rich perovskites (i.e., NaMO_2 F compositions) to not crystallize in a perovskite structure. On the other hand, all NaMOF₂ and Na₂MO₂F compositions have *τ* < 4.18, similar to *t* observations for NaMOF₂ and Na₂MO₂F with *Pbnm* and $P2/b$ groundstates. For Li-TMOF stoichiometries, *τ* predicts none of the Licontaining TMOF compositions to be a perovskite former ([Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S7), partly consistent with the experimental observations of disordered rocksalt or amorphized structures for several Li-TMOFs[.27,30](#page-10-0),[33,34](#page-10-0) Nevertheless, both *t* and *τ* have been developed strictly for $ABO₃$ compositions and primarily to predict their polymorphic stabilities ([Figure](#page-4-0) 3). Since, our

chosen F-rich and O-rich oxyfluorides are not true ABO_3 stoichiometries, particularly the $Na₂MO₂F$ compositions, we have quantified the true thermodynamic (in)stability of the perovskite compositions considered using our calculated *E*hull data (see sections below, Figures 6 and [7](#page-6-0)).

Average Voltages. Figure 5 depicts the calculated average voltages for Na (de)intercalation, versus Na/Na⁺, into the ground state polymorphs of F-rich $MOF₂$ (orange bars) and of O-rich NaMO_2 F (blue bars). The extent of Na (de)intercalation considered in both F-rich and O-rich perovkistes are one Na per f.u., corresponding to $\text{MOF}_2 \leftrightarrow \text{NaMOF}_2$ and $\text{NaMO}_2\text{F} \leftrightarrow \text{Na}_2\text{MO}_2\text{F}$, respectively. Expectedly, we find the F-rich perovskites to exhibit consistently higher average voltages than the corresponding O-rich perovskites, which can be attributed to the greater inductive effect of F[−] compared to O2[−]. [20](#page-10-0) Indeed, fluorine's inductive effect causes an increase in the average voltage of \geq 2 V for all TMs (except Mn at a 1.98 V increase), with the increase in Ni being the highest at 3.08 V.

In both the F-rich and the O-rich perovskites, there is a monotonic increase in voltages along the 3*d* series, with the values increasing from 2.21 V (in Ti) to 4.78 V (Ni) in the Frich and from -0.13 V (Ti) to 2.68 V (Co) in the O-rich perovskites. The monotonic trends in voltages can be largely attributed to the corresponding trends in standard reduction potentials of the TMs.⁶⁸ The dip in voltage from Co to Ni in O-rich perovskites can be primarily attributed to cooperative Jahn−Teller distortion in the Ni-perovskite, which results in larger deviations in the lattice parameters (see compiled *b/a* and *c/a* ratios in Mn- and Ni-perovskites in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S6).

Figure 7. Calculated *E*hull for charged and discharged F-rich TMOFs (bottom two rows) and O-rich TMOFs (top two rows). Each column represents a 3*d* TM, while the *E*^{hull} for each compound is indicated by using text annotations within each square. The green line on the legend bar indicates the 100 meV/atom synthesizability threshold considered in this work.

Interestingly, the average intercalation voltage in the O-rich Tiperovskite exhibits a negative value (-0.13 V) , indicating the nonspontaneity of Na-intercalation in this system. This is because the intercalated $Na₂TiO₂F$ is thermodynamically unstable, with Na metal being one of the decomposition products (see [Figure](#page-5-0) 6).

Given the electrolyte stability windows of liquid electrolytes in NIBs typically span up to 4.8 V vs $\rm Na/Ma^{+09,70}$ $\rm Na/Ma^{+09,70}$ $\rm Na/Ma^{+09,70}$ we find all perovskites considered in this work to be suitable as NIB electrodes. The low average voltages of several O-rich perovskites, including V, Cr, Mn, and Fe (<2.5 V), and $TiOF₂$, make these systems more suitable as possible negative electrode candidates (anodes) than cathodes in a NIB. Thus, based on the voltage data alone, we find the Mn-, Fe-, Co-, and Ni-based F-rich perovskites to be possible candidates for NIB cathodes.

Since an intercalation reaction can often lead to metastable/ unstable products, we can quantify the differences in thermodynamic driving forces between an intercalation reaction and a corresponding "conversion" reaction, following the framework developed by Hannah et al.⁷¹ Thus, we have illustrated a comparison between intercalation and conversion voltages for all perovskites considered in this work in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) [S3](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf). Nevertheless, the practical deployment of any candidate electrode material in NIBs will be highly dependent on their synthesizability (i.e., thermodynamic stability) and rate performance (i.e., Na-ion mobility), which are discussed in the following sections.

Thermodynamic Stability. Upon construction of the quaternary 0 K Na−TM−O−F convex hulls, we plotted pseudoternary slices (or projections) of the quaternary phase diagram for each TM for the ease of visualization. For instance, ternary projections of the Na−Ti−O−F system is displayed in [Figure](#page-5-0) 6, while the ternary projections for the remaining TM systems are compiled in [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S4. The background colors in all panels (shades of green) of [Figure](#page-5-0) 6 indicate the energy of formation (*E*formation), calculated with respect to the terminating compositions of the ternary projections. Stable compounds within the ternary projections are indicated by black circles. Metastable/unstable compounds are indicated by red diamonds. For each metastable/unstable compound among the TMOFs considered, the set of decomposition products (i.e., stable compounds that a metastable/unstable compound

is thermodynamically driven to decompose into) is compiled in [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S8.

For visualizing the $TiOF₂$ composition in the Ti-quaternary, we used a ternary projection terminated by $TiO₂ TiF₃$, and $O₂$ (see [Figure](#page-5-0) 6a). Similarly, for visualizing $NaTiOF₂$, we used the NaTiF₄ $-NaF-Ti₂O₃$ ternary projection ([Figure](#page-5-0) 6b). Both NaTiO₂F and Na₂TiO₂F can be captured within the TiO₂− NaF−Na projection ([Figure](#page-5-0) 6c). Importantly, [Figure](#page-5-0) 6 indicates that $TiOF_2$ is thermodynamically stable ($E^{\text{hull}} = 0$) meV/atom), while NaTiOF₂ and NaTiO₂F are metastable with *E*hull of 46 and 53 meV/atom, respectively, which are below the 100 meV/atom threshold. Also, $Na₂TiO₂F$ is unstable with *E*hull of 187 meV/atom. Notably, Na metal is one of the decomposition products for the unstable $Na₂TiO₂F$ [\(Figure](#page-5-0) [6](#page-5-0)c), which explains the calculated negative intercalation voltage for the NaTiO₂F \leftrightarrow Na₂TiO₂F reaction [\(Figure](#page-5-0) 5).

The heatmap depicted in Figure 7 compiles the *E*hull data of all charged and discharged O-rich and oxo-rich perovskites considered. Blue squares indicate stable/metastable compounds, while red squares indicate unstable compounds. The text annotations within each square represent the E^{hull} in meV/ atom for the corresponding compound. Significantly, we find only TiOF₂ and VOF₂ to be thermodynamically stable (i.e., $E^{hull} = 0$ meV/atom) among all the TMOFs considered. This is in agreement with experimental reports that have synthesized $TiOF₂²⁷$ $TiOF₂²⁷$ $TiOF₂²⁷$ and $VOF₂⁷²$ $VOF₂⁷²$ $VOF₂⁷²$ All charged and discharged compositions of Fe-, Co-, and Ni-based TMOFs are unstable, with *E*hull greater than the synthesizability threshold of 100 meV/atom, citing the high unsuitability of such compositions as NIB electrodes. Moreover, all O-rich perovskites, except NaTiO_2F , exhibit *E*hull > 100 meV/atom, highlighting their high instabilities. Note that tolerance factor estimates, as depicted in [Figure](#page-4-0) 4, do not capture the calculated (in)stability trends accurately since they are designed to predict polymorphic stabilities ([Figure](#page-4-0) 3) and not thermodynamic stabilities, thus signifying the importance of constructing 0 K convex hulls and computing the resulting *E*hull values.

While it is good for an electrode to have thermodynamically stable charged and discharged states to avoid any irreversible decomposition or conversion reactions during an electrochemical cycle, topotactic (de)intercalation is often possible with metastable charged and discharged states as well.^{71,73–[75](#page-11-0)} Thus, compositions that lie within the *E*^{hull} threshold of 100 meV/atom can be considered as possible electrodes. Given our

Figure 8. GGA-calculated *E*^m of pristine (solid orange bars) and strained (solid gray or hashed bars) candidate compositions. The horizontal dotted line indicates a threshold *E*^m of 1000 meV.

stability data, the possible structures that can be considered as NIB electrodes include TiOF₂−NaTiOF₂, VOF₂−NaVOF₂, $CrOF₂$, and NaMnOF₂, and the ease of Na-ion mobility within these frameworks will further determine their suitability. Note that the high instabilities of NaCrOF₂ and MnOF₂ may limit the Na insertion/extraction capacity in these electrodes, compared to the charged−discharged pairs of TiOF2− NaTiOF₂ and VOF₂−NaVOF₂. Although we find NaTiO₂F to be metastable, we did not calculate Na E_m within this structure given the negative average intercalation voltage associated with $Na₂TiO₂F$ formation.

Ionic Mobility. For the candidate compositions identified via our voltage and stability calculations, we estimated the Na *E*^m via the vacancy-mediated mechanism and compiled the values in Figure 8. Barriers calculated in regular TMOF compositions are represented by solid orange bars in Figure 8, while barriers calculated in strained compositions (vide infra) are indicated by solid gray or hatched bars. We used a threshold value of 1000 meV for the $E_{\rm m}$, indicated by the dotted black line in Figure 8, to represent an electrode material that can be used under reasonable electrochemical conditions, similar to our previous works.^{[74,76](#page-11-0)} Thus, electrodes that exhibit $E_{\rm m} \leq 1000$ meV are considered candidates for further experimental exploration. Notably, all short-listed TMOF compositions exhibit barriers that are above the 1000 meV threshold in their pristine state. Only NaTiOF_2 , with a barrier of 1121 meV, is close to the 1000 meV threshold, with other compositions exhibiting significantly higher *E*m, including NaVOF₂ (1486 meV), NaMnOF₂ (1619 meV), TiOF₂ (1709 meV), VOF_2 (2384 meV), and $CrOF_2$ (2570 meV).

Introducing strain in an electrode can often lead to lowering of *E*^m and consequent increasing in ionic mobility.[77](#page-11-0)−[79](#page-11-0) Thus, to examine whether the identified TMOFs can reasonably function as NIB electrodes under strain, we introduced a homogeneous tensile strain of 5% across all lattice parameters of TiOF2 and evaluated the Na-*E*^m values using the GGA-based NEB. To ensure that the tensile strain is maintained during structural relaxation, we restricted the relaxation of the end points to only include changes in ionic positions. Importantly, the strain introduction significantly reduced the *E*^m to 636

meV (i.e., by 62.8%) compared to pristine-TiOF₂, as shown by the solid gray bar in Figure 8.

Assuming similar reductions in calculated E_m with strain addition in other TMOFs (i.e., by 62.8% compared to the pristine-case), we estimate the barriers in strained NaTiOF_2 , $VOF₂$, NaVOF₂, CrOF₂, and NaMnOF₂ to be 417, 888, 553, 957, and 607 meV, respectively (see hashed bars in Figure 8). Thus, all TMOFs identified using our voltage and stability criteria may exhibit reasonable Na-ionic mobility, provided that a homogeneous strain is introduced within the materials. In practice, lattice expansion can be achieved through doping,^{[80](#page-11-0),[81](#page-11-0)} heat/mechanical treatment,^{[82,83](#page-11-0)} and/or epitaxially, such as in the case of thin film electrodes.^{[78](#page-11-0),[84](#page-11-0)} Note that introducing strain and maintaining it during electrochemical cycling may come at the cost of the energy density of the eventual battery. Thus, we expect $TiOF_2-NaTiOF_2$, $VOF_2 NaVOF₂$, $CrOF₂$, and $NaMnOF₂$ to be NIB electrodes worth exploring experimentally, if utilized under strained electrode configurations and thin film batteries.

■ **DISCUSSION**

In this work, we performed first-principles calculations to explore the scope of 3*d* TM-based F- and O-rich perovskite oxyfluorides ($Na_xMOF₂$ and $Na_{1+x}MO₂F$, $x = 0-1$) as NIB electrodes. Using a structural template based workflow, we identified the ground state polymorphs of the charged $MOF₂$ and NaMO₂F compositions ($M = Ti$, V, Cr, Mn, Fe, Co, or Ni) among six possible space groups commonly adopted by perovskites. Subsequently, we introduced Na to create the corresponding discharged perovskite compositions, namely, $NaMOF₂$ and $Na₂MO₂F$, and evaluted the average Na (de)intercalation voltages, 0 K thermodynamic stabilities in all perovskites, and Na-ion mobility in a selected set of candidate perovskites. Based on our voltage, stability, and mobility calculations, we identify six perovskite compositions, namely, TiOF₂−NaTiOF₂, VOF₂−NaVOF₂, CrOF₂, and NaMnOF_2 to hold some promise, alongside challenges, as NIB electrodes, if used in strained configurations and/or in thin film batteries.

During the process of enumerating possible structures for the charged perovskites, we only considered a maximum of 16 lowest electrostatic energy configurations within each space group and identified the ground state configuration among these structures as the one with the lowest DFT total energy (per f.u.). Note that the choice of the 16 lowest electrostatic energy structures (per space group) is an approximation, and there is always a nonzero chance of encountering the "true" ground state beyond this choice. Using our criteria of a maximum of 16 structures per space group contributes to a total of 72 structures per perovskite composition (i.e., $16 \times 4 +$ 5 + 3), which in turn adds up to 1008 structures over all TMs considered and over both O-rich and F-rich compositions, which by itself represents a significant computational expense. Nevertheless, even if the "true" ground state is beyond the set of configurations we have considered here, we expect it to exhibit a lower energy, of the order of ∼10 meV/f.u., compared to the ground state that we have identified, which will only cause a marginal change to the voltage (∼10 mV) and stability $(E^{\text{hull}} \pm 10 \text{ meV/f.u.})$ predictions.

Another approximation in our structure generation workflow is the identification of ground state configurations at the charged perovskite compositions, followed by the addition of Na to the lowest-energy charged structure to obtain the discharged structure. We could have followed a similar procedure of ground state identification using the discharged composition instead of the charged composition. Our choice of the charged perovskite composition for ground state identification was motivated largely by experimental reports on TMOFs in LIBs, wherein, Li was typically inserted into charged TMOF compositions.^{[27,28](#page-10-0)} Thus, the TMOF composition was synthesized first, followed by Li discharge to obtain the discharged state. Considering the ground state configuration at the discharged state may lead to qualitatively different results in terms of average voltages, 0 K stability, and Na-ionic mobility. But considering a workflow along the discharged compositions represents a significant computational effort, which we plan to take up as future work.

In this work, we have restricted our investigation to the 3*d* series despite the possibility that oxyfluoride frameworks may form with second-row TMs (such as Mo and Nb).^{[27](#page-10-0),[85,86](#page-11-0)} Note that TMOFs with 4*d* TMs are likely to exhibit lower Na intercalation voltages compared to the corresponding 3*d* TMs, similar to trends observed in phosphate-based polyanionic cathodes. For example, $Nb_2(PO_4)_3 \leftrightarrow Na_3Nb_2(PO_4)_3$ exhibits a lower 1.46 V_1^{87} V_1^{87} V_1^{87} compared to the analogous $\text{NaV}_2(\text{PO}_4)_3$ $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ that exhibits a higher 3.4 V.^{[88](#page-11-0)} A similar trend is also observed on comparing the Mo (NaMo₂(PO₄)₃ \leftrightarrow $\text{Na}_3\text{Mo}_2(\text{PO}_4)_3$; 2.45 V),^{[89](#page-11-0)} to the Cr $\text{NaCr}_2(\text{PO}_4)_3 \leftrightarrow$ Na₃Cr₂(PO₄)₃; 4.5 V),^{[90](#page-12-0)} phosphate. Nevertheless, 4*d* perovskite-based TMOFs are worth exploring as potential NIB anodes.

We particularly chose the O/F ratios of 1:2 and 2:1 in this we paradomize the $M^{4+}/3+$ redox-couple during Na (de)intercalation. Note that this choice of O:F ratios not only maximizes the voltage (via $M^{4+/3+}$ redox-activity) but also maximizes capacity by enabling the theoretical exchange of 1 mol of Na per TMOF formula unit. Indeed, O:F ratios other than 1:2 or 2:1 will introduce mixed oxidation states of M at the discharged and charged compositions, which will limit the theoretical capacity. Moreover, the computational modeling of O:F ratios other than 1:2 or 2:1 necessitates the usage of larger perovskite supercells (for each space group considered), which significantly increases computational cost per calculation and also increases the number of unique configurations that we will

have to sample to arrive at the ground state configuration. In any case, we have only sampled a sliver of possible chemistries that can be accessed within the TMOF chemical space, and we aim to explore other O:F ratios as part of follow-up work.

For all SCAN+*U* calculations, we used the *U* value derived from TM oxides since the oxide-based *U* better reproduced the experimentally determined voltages for Li-intercalation in TMOFs, such as $VO₂F \leftrightarrow LiVO₂F$ and TiOF₂ \leftrightarrow $Li_{0.5}TiOF_2$ ^{[27,28](#page-10-0)} Hence, we did not tailor our *U* values specifically for oxyfluorides. More experimental data will be needed to verify if such tailored *U* values will yield more accurate predictions. Additionally, we initialized all our TMs in their corresponding ferromagnetic high-spin configurations and did not consider possible magnetic/spin orderings due to their computational complexity, which may have marginally affected the set of ground states that we obtained. Also, SCAN +*U* is known to overestimate intercalation voltages and meta/ instability of compounds, 91 which is also a reason for us to consider a fairly large threshold ($E^{\text{hull}} \leq 100 \text{ meV}$ /atom) for synthesizability.

The metastable compositions of NaTiOF₂, NaVOF₂, and NaMnOF₂ are predicted to decompose to more stable oxides and fluorides. For example, $NaTiOF₂$ should decompose into $Ti₂O₃$, NaTiF₄, and NaF (see [Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S8), all of which are solid phases consisting of a single anion (i.e., oxygen or fluorine). This type of solid-state decomposition reaction that involves phase separation within the anionic entity (i.e., formation of oxides and fluorides from oxyfluorides) is expected to be slow, since this will involve the diffusion of anionic species in addition to the cations. $92-94$ $92-94$ $92-94$ Thus, we expect NaTiOF₂, $NaVOF₂$ and $NaMnOF₂$ to remain metastable under typical electrochemical conditions. Additionally, if decomposition indeed occurs, electrochemically active decomposition products like Ti_2O_3 ^{[95](#page-12-0)} NaTiF₄,^{[96](#page-12-0)} V₂O₃,^{[23](#page-10-0)} Na₃VF₆²³ or Na₃MnF₆^{[97](#page-12-0)} which have open channels for Na migration, may participate as (de)intercalation frameworks, thus contributing to electrochemical activity. Hence, careful characterization of the electrochemical performance of TMOFs may be necessary to ensure that any observed activity is indeed due to the exchange of Na with the TMOF framework.

In the case of metastable-CrOF₂, the structure is predicted to form O_2 gas as a decomposition product [\(Table](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S8), which can entropically drive the decomposition reaction. While O_2 evolution during synthesis can be mitigated by increasing the partial pressure of $O_2^{98,99}$ $O_2^{98,99}$ $O_2^{98,99}$ $O_2^{98,99}$ $O_2^{98,99}$ preventing O_2 evolution during electrochemical cycling may be challenging.^{[100](#page-12-0)} Moreover, we observed all of the discharged phases of the O-rich oxyfluorides (Na2MO2F) are unstable with significantly higher *E*hull than 100 meV/atom. Perhaps, the increase in electrostatic repulsion due to inserting two Na ions into the A-site of the perovskite framework might have affected stability and is reflected by the high *E*^{hull} values observed in Na₂MO₂F, which further supports the idea that these materials may not be practically viable.

We used a reasonably high threshold for ionic mobility (E_m $\leq 1000 \text{ meV}^{74}$) to identify candidates partly due to the limited literature on Na-ion mobility within crystalline ordered oxyfluorides. Moreover, the addition of F[−] to oxides can result in a reduction of Na+ mobility due to more ionic Na−F bonds than Na−O, similar to observations of reduction in Li-mobility in F-doped oxide-based disordered rocksalts.^{[101](#page-12-0),[102](#page-12-0)} Importantly, our calculations indicated that only NaTiOF₂ (E_m = 1121 meV) came close to the threshold used, with all other oxyfluorides considered exhibiting significantly high *E*^m for Namotion. We observe that Na⁺ has to migrate via a tetrahedral void sandwiched between two Na−O−F polyhedra in the perovskites considered, i.e., *Pbnm*-based TiOF₂−NaTiOF₂ and VOF2−NaVOF2, and *R3*̅*c*-based CrOF2 and NaMnOF2, which may contribute to the observed high E_m in these structures.^{[103](#page-12-0)} However, introducing a homogeneous strain (∼5%) within the lattice can significantly reduce the *E*^m (by ∼60%), as demonstrated for the case of $TiOF₂$, due to the expansion of the transition state (see [Figure](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf) S6). Thus, TMOFs can exhibit reasonable rate performance under lattice strain. However, the need to maintain the strained structure may limit the applicability of TMOFs to low power and/or thin film batteries that are typically used in Internet-of-things applications and wearable electronics.

Considering the oxyfluoride compositions of Na_xMOF₂ and $Na_{1+x}MO₂F$ was primarily motivated by the availability of the M4+/3+ redox couple, which is exhibited by several 3*d* TMs, quite reversibly. Our work can be extended to other fluorineadded compositions, such as F-substituted oxides, phosphates, sulfates, and pyrophosphates. Indeed, high voltages and capacities with Na (de)intercalation have already been reported in fluorophosphates.[104](#page-12-0)−[106](#page-12-0) Therefore, we are hopeful that our research lays the foundation for exploring other promising compositions for NIB electrodes within and beyond the chemical space of oxyfluorides.

■ **CONCLUSION**
NIBs, which represent an alternative technological pathway to state-of-the-art LIBs in energy storage technology, require novel materials to improve the energy and power densities so that NIBs compete better with LIBs. Here, we explored the chemical space of perovskite-based TMOFs, considering both the O-rich and F-rich compositions as possible Na-ion intercalation hosts. Specifically, we performed DFT-based calculations on Na_xMOF_2 and $\text{Na}_{1+x}\text{MO}_2\text{F}$ ($x = 0-1$), where M = Ti, V, Cr, Mn, Fe, Co, or Ni, evaluating the ground state polymorphs, average Na (de)intercalation voltages, 0 K stabilities, and Na⁺ mobilities. We found that F-rich perovskites exhibit higher voltages than O-rich compositions due to the stronger inductive effect of F[−]. In terms of stability, only $TiOF₂$ and $VOF₂$ were stable, while other compositions, including NaTiOF₂, NaVOF₂, CrOF₂, and NaMnOF₂ were metastable (*E*hull ≤ 100 meV/atom). However, all stable and metastable TMOFs exhibited a high *E*^m (≥1000 meV) for Na+ motion in their pristine states. Nevertheless, introducing a 5% homogeneous tensile strain causes the *E*^m to drop by ∼60% compared to the pristine state, suggesting that the TMOFs may have applications in thin film batteries and in strained electrode configurations. Our study represents a systematic computational exploration of the oxyfluoride chemical space, which we hope will reinvigorate research in these chemistries for NIBs and beyond.

■ **ASSOCIATED CONTENT**

Data Availability Statement

The data that support the findings of this study are openly available at our [GitHub](https://github.com/sai-mat-group/na-oxyfluorides/) repository.

\bullet Supporting Information

The Supporting Information is available free of charge at [https://pubs.acs.org/doi/10.1021/acs.chemmater.4c02374](https://pubs.acs.org/doi/10.1021/acs.chemmater.4c02374?goto=supporting-info).

> Details of PAW potentials used, description of site determination for introducing additional Na in perov

skites, compilation of 0 K phase diagrams, conversion voltages, and the associated stability data, and all calculated MEPs ([PDF\)](https://pubs.acs.org/doi/suppl/10.1021/acs.chemmater.4c02374/suppl_file/cm4c02374_si_001.pdf)

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Notes

The authors declare no competing financial interest.

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