

Kinetic Monte Carlo Simulations of Sodium Ion Transport in NaSICON Electrodes

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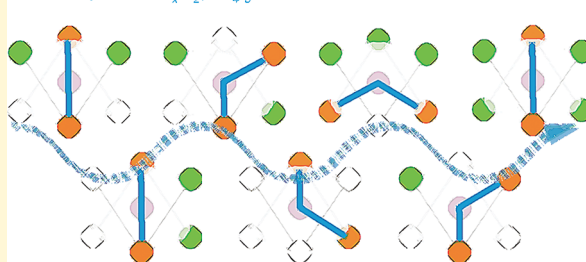
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ABSTRACT: The development of high-performance sodium (Na) ion batteries requires improved electrode materials. The energy and power densities of Na superionic conductor (NaSICON) electrode materials are promising for large-scale energy storage applications. However, several practical issues limit the full utilization of the theoretical energy densities of the NaSICON electrodes. A pressing challenge lies in the limited sodium extraction in low Na content NaSICONs, e.g., $\text{Na}_1\text{V}^{\text{IV}}\text{V}^{\text{IV}}(\text{PO}_4)_3 \leftrightarrow \text{V}^{\text{V}}\text{V}^{\text{IV}}(\text{PO}_4)_3 + \text{e}^- + \text{Na}^+$. Therefore, it is important to quantify the Na-ion mobility in a broad range of NaSICON electrodes. Using a kinetic Monte Carlo approach bearing the accuracy of first-principles calculations, we elucidate the variability of Na-ion transport vs Na content in three important NaSICON electrode materials, $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$. We show Na^+ transport in NaSICON electrode materials is almost entirely determined by the local electrostatic and chemical environment set by the transition metals and the polyanionic scaffold. The competition with the ordering-disordering phenomena of Na vacancies also plays a role in influencing Na transport. We identify the Na content providing the highest room-temperature diffusivities in these electrodes, i.e., $\text{Na}_{2.7}\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_{2.9}\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_{2.6}\text{Cr}_2(\text{PO}_4)_3$. We link the variations in the Na^+ kinetic properties by analyzing the competition of ligand field stabilization transition metal ions and their ionic radii. We interpret the limited Na extraction at $x = 1$ observed experimentally by gaining insights into the local Na vacancy interplay. Targeted chemical substitutions of transition metals disrupting local charge arrangements will be critical to reducing the occurrence of strong Na^+ -vacancy orderings at low Na concentrations, thus expanding the accessible capacities of these electrode materials.

Na⁺ transport in Na_xM₂(PO₄)₃ M = Ti, V and Cr via kinetic Monte Carlo



1. INTRODUCTION

Having achieved widespread commercialization, rechargeable lithium (Li)-ion batteries (LIBs) are now at the risk of geopolitically constrained supply chains of key raw materials, such as cobalt, nickel, and Li.^{1–3} Sodium (Na)-ion batteries (SIBs) appear to be promising alternatives to the LIB analogs, as Na-metal can be harvested directly from seawater.^{4–6} Extensive research is underway to optimize electrodes and electrolytes for SIBs.^{7–21} One of the material classes for NIBs is the polyanionic sodium superionic conductor (NaSICON), discovered by Hong et al.,^{22,23} a framework studied for its fast Na-conducting properties. Electrodes crystallizing in the NaSICON framework, with formula $\text{Na}_x\text{M}_2(\text{PO}_4)_3$ (where M = transition metal), can be highly tuned to achieve promising energy densities,^{10,14,24} by changing the ratio and types of transition metals in the NaSICON, such as $\text{Na}_x\text{TiV}(\text{PO}_4)_3$, $\text{Na}_x\text{TiMn}(\text{PO}_4)_3$, $\text{Na}_x\text{VMn}(\text{PO}_4)_3$, and $\text{Na}_x\text{CrMn}(\text{PO}_4)_3$.^{10,13}

For most NaSICON electrodes, the accessible capacity is significantly lower than the theoretical value, which is linked to difficulties in reversibly extracting the entire available Na

content. For example, in $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, the reversible extraction of four sodium ions entails the utilization of all vanadium redox states ($\text{V}^{\text{V}}/\text{V}^{\text{IV}}$, $\text{V}^{\text{IV}}/\text{V}^{\text{III}}$, and $\text{V}^{\text{III}}/\text{V}^{\text{II}}$) with a theoretical gravimetric capacity of $\sim 235 \text{ mAh g}^{-1}$. In practice, only two sodium ions can be reversibly extracted from $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ up to $\text{Na}_1\text{V}_2(\text{PO}_4)_3$.^{14,15,24–26} While Gopalakrishnan and Rangan suggested the possibility of chemically extracting the last Na^+ forming $\text{V}_2(\text{PO}_4)_3$,²⁷ successive endeavors have proven unsuccessful. Hence, understanding the factors that limit reversible Na extraction within NaSICONs and facilitating the same remains an active topic of research.

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In this Letter, using density functional theory (DFT) based kinetic Monte Carlo (kMC) simulations, we unveil the physical origins for the variation in Na⁺ transport properties in three NaSICON electrode materials, namely, Na_xTi₂(PO₄)₃, Na_xV₂(PO₄)₃, and Na_xCr₂(PO₄)₃. Our analysis reveals the kinetic limits to reversibly extracting Na ions in these NaSICONs apart from identifying the Na-composition ranges to achieve a high Na⁺ diffusivity. The macroscopic Na⁺ transport is highly influenced by the interplay between Na-vacancy arrangements and transition metals. Our results shed light on the optimization of NaSICON electrodes for improved reversible capacities.

2. RESULTS

To investigate the Na⁺ transport in Na_xTi₂(PO₄)₃, Na_xV₂(PO₄)₃, and Na_xCr₂(PO₄)₃, we rely on a combination of DFT calculations, constructing a cluster expansion Hamiltonian, and performing kinetic Monte Carlo simulations (*vide infra*).^{28,29} The ground-state structures representing specific Na-vacancy arrangements at different Na compositions of the Na_xTi₂(PO₄)₃, Na_xV₂(PO₄)₃, and Na_xCr₂(PO₄)₃ NaSICON were taken from refs 10 and 14. To estimate the Na⁺ migration barriers in the three NaSICONs, we selected several sodium compositions, including $x = 1, 3,$ and 4 in Na_xTi₂(PO₄)₃; $x = 1, 2, 3,$ and 4 in Na_xV₂(PO₄)₃; and $x = 1$ and 3 in Na_xCr₂(PO₄)₃.

At $x = 1$ and 4 , all three NaSICONs crystallize in the rhombohedral space group ($R\bar{3}c$ or $R\bar{3}$). While Na₄Cr₂(PO₄)₃ is included for completeness in this investigation, it is not expected to be stable (due to the instability of Cr^{II} in the solid state³⁰) and has never been reported experimentally. Na₃M₂(PO₄)₃ configurations with monoclinic (Cc or $C2/c$) symmetry represent the compositions with the lowest formation energies in the Na_xM₂(PO₄)₃ pseudobinary tie line of all the three NaSICONs.^{10,14} Recent investigations predicted the mixed-valence Na₂V₂(PO₄)₃ as a thermodynamically stable phase.^{14,24}

Each Na-vacancy (Va) configuration at the above Na compositions was optimized using the strongly constrained and appropriately normed exchange and correlation functional within DFT.³¹ A Hubbard U correction (SCAN+ U) was applied, which has been confirmed to accurately predict the redox electrochemistry during Na (de)intercalation.^{14,29,30,32,33} We use the nudged elastic band (NEB) method to simulate the Na⁺ migration barriers.³⁴

Typically, the migration mechanism of ions in fast conductors is ascribed to be a local property of the immediate chemical environment of the migrating species, which is strongly influenced by the local ion-vacancy configuration(s).^{28,29,35,36} Figure 1 shows the relevant local portion of the NaSICON structure—the migration unit (MU)—that is sufficient to capture the Na migration with variations in the local configurations of Na and vacancies. Figure 1a represents the general MU in Na_xM₂(PO₄)₃, where groups of corner-shared octahedra contain six Na(2) sites centered around a Na(1) site. For the sake of visualization, the MO₆ and the PO₄³⁻ groups are not shown. Within each MU octahedron, two Na(2) sites will be “active”, taking part in the Na(2)↔Na(1)↔Na(2) migration event, whereas the remaining four Na(2) sites and/or vacancies will be “inactive” (Figure 1a) and spectating the process of Na migration. Herein, we consider a single Na migration hop Na(2)↔Na(1) as the fundamental Na-ion migration event in a single MU.^{22,23,26,29,37,38}

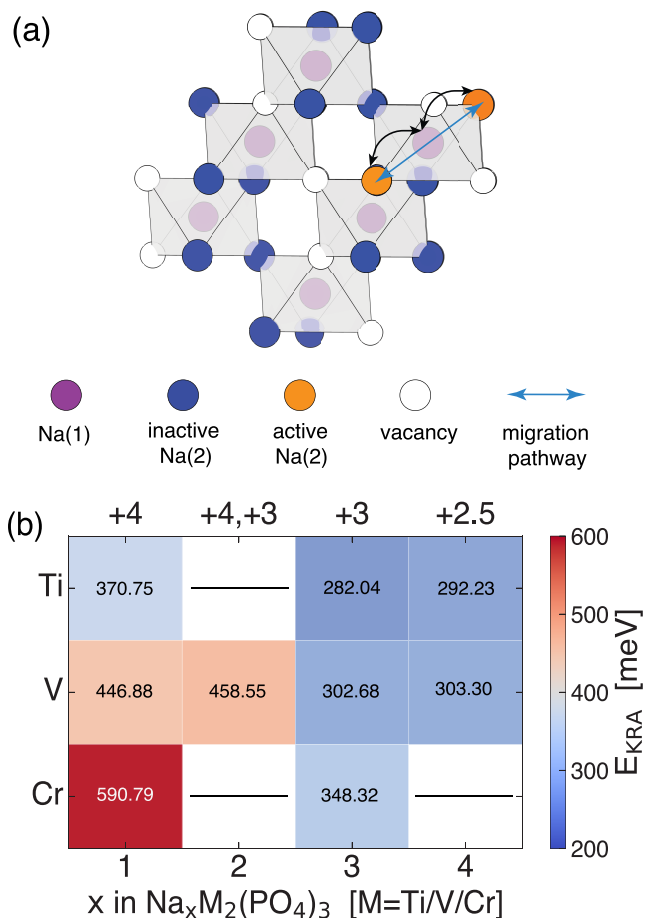


Figure 1. Model of Na⁺ migration in the NaSICON Na_xM₂(PO₄)₃, identifying the migration unit (MU) and associated Na-ion migration barriers. (a) A representation of the Na-vacancy sublattice in NaSICON, illustrated by the corner-sharing octahedra. Two Wyckoff positions, the Na(1) (6b) sites, are shown by purple circles and the Na(2) (18e) sites by orange or blue circles, depending on the participation of the Na(2) site in a migration event. Empty circles denote vacancies. Each Na(1) site is surrounded by six nearest neighbor Na(2) sites. In each octahedron, two Na(2) sites participate in the Na-ion migration pathway (orange circles connected by blue line), whereas every single hop Na(2)↔Na(1) is denoted by the black double-arrows. (b) Computed E_{KRA} 's for the migration event Na(2)↔Na(1) in the MU (values are indicated in each box), with varied Na compositions (x) and transition metals (M). Black lines indicate compositions where migration barriers were not computed (see the main text). Na compositions are shown in the bottom x axis, and the formal oxidation states of the transition metals are in the top x axis.

The collective diffusion of Na ions in the NaSICON electrodes can be captured by our lattice model, which is composed of thousands of MUs, with different Na-vacancy orderings. Indeed, ensembles of MUs are used to tessellate periodically the Na_xM₂(PO₄)₃ structures in the composition range $1 \leq x \leq 4$. At intermediate compositions ($1 < x < 4$), a variety of MUs with different local Na vacancy arrangements is sufficient to approximate the migrating environments of the Na ions. The subsets of crystallographic sites of the migrating Na ions are fully encompassed by an ensemble of MUs incorporating all possible Na-vacancy occupation arrangements. Therefore, the partial occupations of Na sites as refined

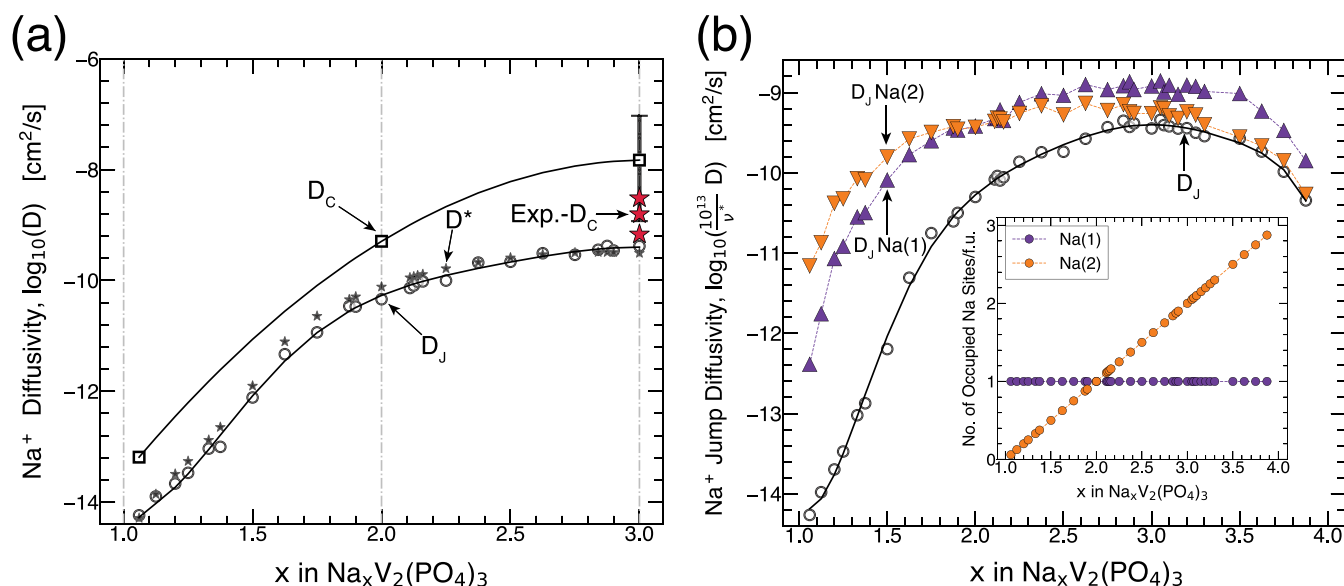


Figure 2. Predicted diffusivities of $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ at 300 K. Panel a plots D_J (circles), D^* (stars), and D_C (squares). The pre-exponential factor is assumed as 1×10^{13} Hz.³⁵ Vertical lines represent the phase boundaries derived from the phase diagram at ~ 300 K.¹⁴ Values of D_C are only in the single-phase regions, i.e., $x = 1, 2,$ and 3 . At intermediate compositions (two-phase regions), the thermodynamic factor $\Theta = 0$ leads to zero D_C . In the two-phase regions, D_C is approximated using Vegard's law. The standard deviation of our predictions is shown at $x = 3.0$. Solid lines in black are the polynomial model fitted on the predictions. The experimental values of chemical diffusivity (exp.- D_C , red stars) are from ref 47 at $x = 3$. Panel b plots D_J (black circles), $D_J\text{Na}(1)$, which arises from the Na(1)-ion movement (purple triangles), and $D_J\text{Na}(2)$ from the Na(2)-ion movement (orange triangles). In panel b, all D_J 's are renormalized with a $10^{13}/\nu^*$ factor, due to the uncertainty in the prefactor ν^* .^{35,48} The inset shows the computed occupation number of Na(1) (in purple) and Na(2) (in yellow) sites per formula unit vs. x extracted from the kMC simulations at 300 K.

from experimental techniques, such as X-ray diffraction,^{14,24,39,40} can be described by the 3D networks formed by thousands of MUs.

Based on the assumption that the transport property relies mainly on the local Na-vacancy orderings, all possible migration pathways within the MUs were extensively simulated using the NEB method combined with SCAN+ U calculations. The computed migration barriers are reported in Section 1 of the Supporting Information (SI). We did not evaluate the migration energy of Na^+ at $x = 2$ in $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$ and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$, as well as at $x = 4$ in $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$, since they have not been reported experimentally.

The computed migration barrier (E_{barrier}) results are in good agreement with prior computational and experimental studies (see section 1 of the SI). For example, for $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3$, the $E_{\text{barrier}} \sim 621$ meV agrees well with the ~ 620 meV experimental value for the α phase of the same system.¹⁶ Similarly, for $\text{Na}_3\text{V}_2(\text{PO}_4)_3$, we predict an $E_{\text{barrier}} \sim 455$ meV, which is comparable with the range of values 353–513 meV computed with the HSE06 functional.⁴¹ In the case of $\text{Na}_3\text{Ti}_2(\text{PO}_4)_3$, the predicted $E_{\text{barrier}} \sim 530$ meV underestimates the experimental value of ~ 750 meV from ref 39.

The directional dependence of E_{barrier} is removed by using the kinetically resolved activation barriers (E_{KRA}), as defined in ref 35. Low values of E_{KRA} correspond to low migration barriers and vice versa. The computed E_{KRA} values of Na^+ migration events of the type $\text{Na}(2) \leftrightarrow \text{Na}(1)$ of an MU that best represents the ground state configurations at different x are shown in Figure 1b. The lowest values of E_{KRA} are calculated at compositions $\text{Na}_3\text{M}_2(\text{PO}_4)_3$ and follow the order $\text{Ti} \sim 282$ meV $<$ $\text{V} \sim 303$ meV $<$ $\text{Cr} \sim 348$ meV. In contrast, the maximum E_{KRA} values are observed at $x \sim 1$, in agreement with existing reports.^{16,26,39} The barriers at $x = 3$ across the

different NaSICONs follow the ligand field stabilization energies (LFSE) for $\text{Ti}^{\text{III}}(d^1) < \text{V}^{\text{III}}(d^2) < \text{Cr}^{\text{III}}(d^3)$, and the decreasing order of the transition metal sizes.^{42,43} Note that LFSE also correlates with the NaSICON pseudobinary formation energies $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3 \gg \text{Na}_3\text{V}_2(\text{PO}_4)_3 > \text{Na}_3\text{Ti}_2(\text{PO}_4)_3$, thus increasing the Na migration barriers in the same order.¹⁰

Starting from the computed E_{KRA} encompassing several Na-vacancy arrangements in the MU (see section 2 of the SI), a local cluster expansion (LCE) Hamiltonian³⁵ was trained for each NaSICON system. We use the LCE together with our kinetic Monte Carlo simulation package⁴⁴ to investigate the Na^+ transport within the NaSICON structures (see sections 2 and 3 in the SI), by performing long-time (on the order of milliseconds) and large-scale ($8 \times 8 \times 8$ formula units corresponding to 4096 Na sites) simulations. The LCE Hamiltonian could investigate Na^+ benchmarked on barriers obtained from first-principles calculations. The accuracy of predicted E_{KRA} 's, obtained from the LCE formalism is bound within root mean square (RMS) errors of ± 31.75 meV for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, ± 25.29 meV for $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, and ± 35.81 meV for $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ (see section 2 in the SI), which are within the perceived accuracy of migration barriers computed from first principles (± 50 meV).⁴⁵

By tracking all possible Na migration events of each NaSICON, we simulated the Na^+ diffusion, quantified by (i) the jump diffusivity (D_J), (ii) the tracer diffusivity (D^*), and (iii) the chemical diffusivity (D_C).³⁶ From the temperature vs composition phase diagrams of these NaSICON systems,¹⁴ using canonical Monte Carlo simulations, 1850 initial Na-vacancy configurations for each system (50 different configurations at 37 unique Na compositions) with specific Na-vacancy arrangements were generated at ~ 973 K, which is

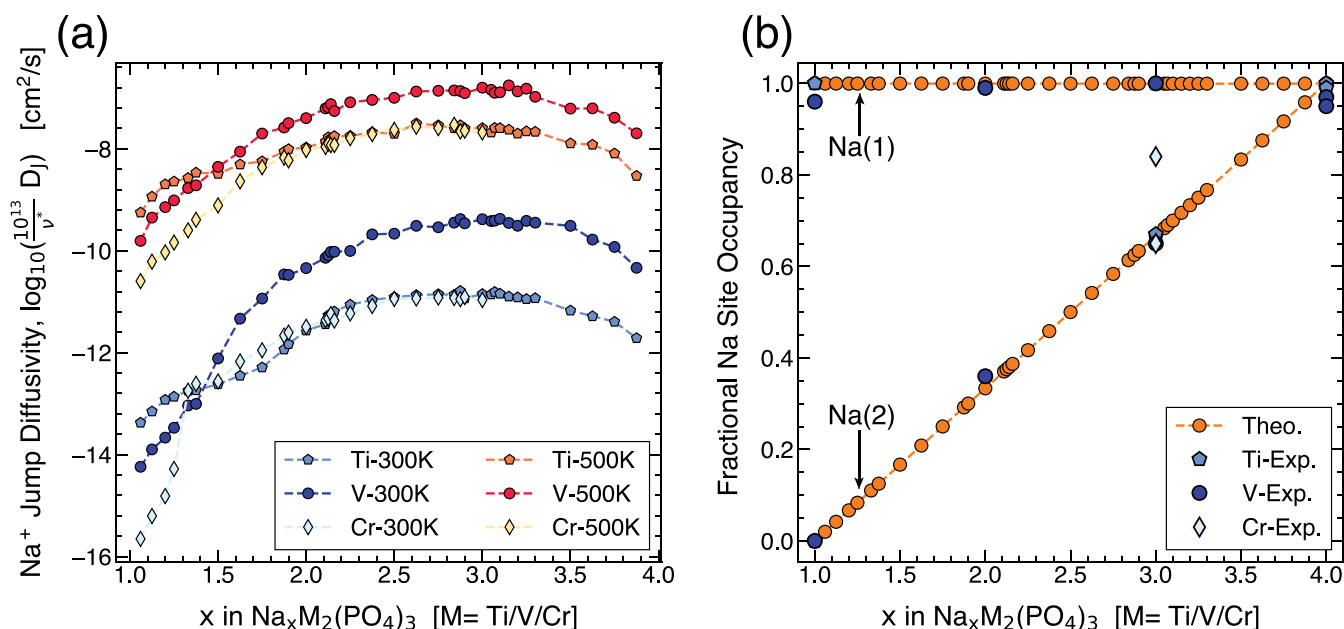


Figure 3. Computed Na^+ D_j at 300 and 500 K (panel a) and fractional occupancy at 300 K (panel b) of Na(1) and Na(2) sites in $\text{Na}_x\text{M}_2(\text{PO}_4)_3$ (M = Ti, V, or Cr). Due to the uncertainty in the prefactor ν^* , all D_j values are normalized using a $10^{13}/\nu^*$ factor. In panel a, data at 300 and 500 K are shown in blue and red/yellow symbols. For $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$, Na extraction can only occur for $1 \leq x \leq 3$.¹⁷ The computed results (Theo.) in panel b are denoted by orange circles, with experimental values in blue shapes.^{15,18,24,52,53} The computed Na-site occupancy does not show significant differences among the three NaSICONs within our predictions; hence, data for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ is plotted in panel b.

the typical synthesis temperature of these NaSICONs. Thus, these model structures mimic Na-vacancy configurations that are obtained postsynthesis^{17,22–24,26,46} and are used in the kMC simulations as starting configurations. Subsequently, we performed 500 equilibration sweeps: one sweep is the total number of Na-vacancy sites in the simulation model, i.e., 4096 followed by 3000 kMC sampling sweeps of each configuration and statistically averaged the transport properties over a wide temperature range (300 to 900 K, see section 3 of the SI).

We used $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ to discuss the behavior of the diffusion coefficients predicted by our kMC simulations. Figure 2a shows the computed D_j , D^* , and D_C values for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ at 300 K as a function of x .

We derived the D_j by tracking the center-of-mass of all of the migrating Na^+ species, including the cross-correlations between different Na ions, which are excluded in the tracer diffusivity D^* . For this reason, in Figure 2a, D_j and D^* are different, but of similar magnitude, highlighting minimal contributions from cross-correlations, similar to observations in other electrode materials.³⁵ From the statistical analysis of the computed diffusivities, we derived a standard deviation (Figure 2a) of approximately ± 1 order of magnitude in diffusivity (± 120 meV in terms of E_{barrier}).⁴⁵

In $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, the Na^+ jump diffusivities of Figure 2a increase progressively from low Na content ($\sim 5.77 \times 10^{-15}$ cm² s⁻¹ at $x \sim 1$) to high Na content ($\sim 4.16 \times 10^{-10}$ cm² s⁻¹ at $x = 3.0$). Diffusivities for $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ are in good agreement with existing measurements.^{26,38,49}

We derive a fourth order polynomial fit for the monotonically increasing D_j across $1 \leq x \leq 3$, namely, $D_j(x) = C + E_1x + E_2x^2 + E_3x^3 + E_4x^4$ (black line in Figure 2). The coefficients of the fit E_1 , E_2 , E_3 , and E_4 are reported in the SI. The fitted polynomial reflects the concentration dependence of D_j .

The chemical diffusivity D_C depends on the thermodynamic factor Θ , as per $D_C = D_j\Theta$; values of Θ are from ref 14. D_j and Θ contribute oppositely to D_C . As Θ is related to the gradient of the Na chemical potential (eq 13 in SI), Θ usually takes large values for highly ordered (stable) configurations (Supporting Figure 16 in the SI), increasing the D_C of the corresponding ordered phase. In contrast, low values of D_j are typically found in ordered phases due to a lack of accessible vacant sites controlled by strong ion-vacancy ordering interactions. In $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, D_C is dominated by D_j , as denoted by the relatively low values of room temperature chemical diffusivity at $x = 1$ and 2 (instead of the large values as controlled by Θ).³⁵ Gray vertical lines in Figure 2a depict the phase boundaries for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ from ref 14 at 300 K. The predicted values of D_C at $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ (1.18×10^{-9} to 9.35×10^{-8} cm² s⁻¹) are higher than the experimental values (4.59×10^{-10} to 2.0×10^{-9} cm² s⁻¹) measured by electrochemical impedance spectroscopy (EIS).^{38,47}

While some experimental values of D_C ^{38,47} fall within the standard deviations of our predictions, other experimental studies have reported significantly different D_C values, such as 3×10^{-15} and 6×10^{-13} cm² s⁻¹ measured using the galvanostatic intermittent titration technique (GITT),⁵⁰ and 4×10^{-14} to 2.48×10^{-13} cm² s⁻¹ measured by EIS.⁵¹ Such large differences in experimental D_C values can be attributed to different synthesis procedures of $\text{Na}_3\text{V}_2(\text{PO}_4)_3$, which can affect the (im)purity of the particles, the particle sizes, and the defect concentrations, thus causing significant variations in transport properties.³⁸ Nevertheless, we expect our kMC simulations to yield an accurate value of D_C within bulk $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ given that our confidence interval of calculated D_C is quite narrow.

The computed D_C for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ at 300, 700, and 900 K (Supporting Figure 17 of the SI) is superimposed on the

temperature–composition phase diagram,¹⁴ where the single-phase regions are always connected by dashed lines representing the two-phase regions. For all temperatures explored, we observe an increase in D_C in the composition range $1 \leq x \leq 3$. Unsurprisingly, the D_C values increase for increasing temperatures (i.e., at $x = 3$ from $1.48 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$ at 300 K to $2.5 \times 10^{-3} \text{ cm}^2 \text{ s}^{-1}$ at 900 K), signifying high thermally activated motion of Na^+ .

Given the dominating contributions of D_j to the effective chemical diffusivity,³⁶ we can gain valuable insights about the jump diffusivity (D_j) of $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ at 300 K by separating D_j into the specific contributions from each sodium site, i.e., Na(1) and Na(2) in Figure 2b. Here, we obtain $D_j\text{Na}(1)$ in the $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ structure by tracking all unique Na^+ hopping events of the type $\text{Na}(1) \rightarrow \text{Na}(2)$, while we track $\text{Na}(2) \rightarrow \text{Na}(1)$ for $D_j\text{Na}(2)$. The differences between the overall D_j and individual $D_j\text{Na}(1)$ and $D_j\text{Na}(2)$ originate mainly from the number of the Na(1) and Na(2) sites available (see eqs 8, 9, and 10 in SI).

Values of $D_j\text{Na}(2)$ and $D_j\text{Na}(1)$ show similar magnitudes and appear higher than the overall D_j , especially in the composition range $1 \leq x \leq 3$. Both the $D_j\text{Na}(1)$ and $D_j\text{Na}(2)$ achieve their maxima at intermediate Na compositions, specifically $1.21 \times 10^{-9} \text{ cm}^2 \text{ s}^{-1}$ at $x \approx 2.94$ for $D_j\text{Na}(1)$ and $1.15 \times 10^{-9} \text{ cm}^2 \text{ s}^{-1}$ at $x \approx 2.71$ for $D_j\text{Na}(2)$. We observe a sharp decrease of Na diffusivity near $x \sim 1$, where values $D_j\text{Na}(2)$ and $D_j\text{Na}(1)$ are $6.91 \times 10^{-12} \text{ cm}^2 \text{ s}^{-1}$ and $4.11 \times 10^{-13} \text{ cm}^2 \text{ s}^{-1}$, respectively.

The number of occupied Na sites extracted from kMC simulations (inset of Figure 2b) agrees well with existing site occupations at 300 K from experiment and theory.^{14,24} Na(1) sites (purple line) are always fully occupied in the range $1 \leq x \leq 3$, whereas the Na(2) occupation (orange) varies from empty at $x = 1$ to fully occupied, with three Na(2) sites per formula unit at $x = 4$. The number of occupied Na(2) sites is much lower than that of Na(1) at compositions around $x = 1$,¹⁴ reflecting the difference in stability of the two sites at $x = 1$, which results in boosting the $D_j\text{Na}(2)$ over $D_j\text{Na}(1)$. Effects of cross-correlations among Na ions distributed between Na(1) and Na(2) sites remain convoluted in the computed values of D_j .

We discuss the kMC predictions of two additional NaSICONs, $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$, with similar electrochemical behavior to $\text{Na}_x\text{V}_2(\text{PO}_4)_3$.^{10,14–18} For $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, the sodium composition ranges $1 \leq x \leq 3$ and $3 \leq x \leq 4$ are accessible electrochemically,^{10,18} whereas for $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$, Na extraction only occurs in $1 \leq x \leq 3$.^{10,17} Similar to $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ show single phases at $x = 1$ and $x = 3$.^{10,17,18,52,53} Figure 3a shows the computed D_j of $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ at 300 and 500 K.

For all systems, we observe an increase of D_j in the composition range $1 \leq x \leq 3$, followed by a gradual decrease of D_j for $3 < x \leq 4$ in $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$ and $\text{Na}_x\text{V}_2(\text{PO}_4)_3$. At 300 K, D_j reaches a maximum for all systems at $x \sim 3$, with $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ displaying a higher magnitude of D_j in the range $1.5 \leq x \leq 4$ than $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$ and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$. At 500 K, in comparison, the D_j values of all three NaSICONs were of a similar order of magnitude, corresponding intuitively to higher diffusion rates with increasing temperatures.

The maximum values of D_j occur at similar compositions for all NaSICONs, $4.09 \times 10^{-10} \text{ cm}^2 \text{ s}^{-1}$ for $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ at $x \sim 2.9$, $1.71 \times 10^{-11} \text{ cm}^2 \text{ s}^{-1}$ for $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$ at $x \sim 2.7$, and

$1.39 \times 10^{-11} \text{ cm}^2 \text{ s}^{-1}$ for $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ at $x \sim 2.6$, respectively. Similarly, the lowest values of D_j occur at a low Na content (i.e., $x \sim 1$) for all NaSICONs. For example, the lowest D_j among the NaSICONs at $x \sim 1$ is $2.2 \times 10^{-16} \text{ cm}^2 \text{ s}^{-1}$ for $\text{Na}_1\text{Cr}_2(\text{PO}_4)_3$. The low values of D_j at $x \sim 1$ suggest that the reversible extraction of the “last” Na ion from NaSICON electrodes may be limited also by the poor kinetics at low Na contents.

To understand the Na^+ distributions at 300 K, we extract the fractional occupancies of Na(1) and Na(2) sites (Figure 3b) and compare them with the experimental data of these NaSICON systems. At room temperature, we observe high stability of the Na(1) site across the entire Na concentration range ($1 \leq x \leq 4$), where it remains fully occupied, while Na(2) occupancy monotonically increases with increasing x . Our kMC results agree quantitatively with the experimentally refined Na(1)/Na(2) occupations.^{15,18,24,52,53} In the case of $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3$, the predicted occupation of Na(1) (~ 1) overestimates the experimental data (~ 0.84), which suggests that the nominal composition may deviate from the real composition of synthesized NaSICONs.⁵³

3. DISCUSSION

In this Letter, using kMC simulations that bear the accuracy of DFT calculations, we investigated the variability of Na-ion transport vs Na content in three important NaSICON electrodes for Na-ion batteries: $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$. We demonstrated that the ion transport properties (D_j , D^* , and D_C) of NaSICONs have a configurational dependence on the local sodium vacancy arrangements near the migration events.

In the three NaSICONs, we observed an increase of D_j from low Na concentrations of $x \sim 1$ to $x \sim 3$. For $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ and $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, we observed a decrease in D_j in the composition range $3 < x \leq 4$ (Figure 3a).

Interplay of Ligand Field Stabilization and Ionic Radii of Transition Metals. Two main factors: (i) the ligand field stabilization of transition metals and their (ii) ionic radii, can explain variations of migration barriers and diffusivities in these NaSICONs as a function of Na composition.

Different NaSICONs exhibit different migration barriers at the same Na content (see Figure 1b), with implications for the observed D_j . For example, at $x \sim 1$, the highest $E_{\text{KRA}} \sim 591$ meV is exhibited by $\text{Na}_1\text{Cr}_2(\text{PO}_4)_3$, well exceeding 447 meV in $\text{Na}_1\text{V}_2(\text{PO}_4)_3$, and 371 meV in $\text{Na}_1\text{Ti}_2(\text{PO}_4)_3$. Since at $x \sim 1$ all transition metals, Cr, Ti, and V, are tetra-valent (verified by the magnetic moments of Supporting Figure 7 in the SI), differences in migration energies in NaSICONs at this composition are controlled by the transition metal ionic radii, which will lead to different sizes of “bottlenecks” for the migrating Na ion.²⁴

At $x = 1$, the transition metal ionic radii follow the trend of $\text{Ti}^{\text{IV}} (\sim 0.61 \text{ \AA}) > \text{V}^{\text{IV}} (\sim 0.58 \text{ \AA}) > \text{Cr}^{\text{IV}} (\sim 0.55 \text{ \AA})$, which causes a similar variation in the lattice parameters.^{10,24,52} Thus, the sizes of the bottlenecks (i.e., the transition state) for the migrating Na^+ reduce in the order of $\text{Na}_1\text{Ti}_2(\text{PO}_4)_3 > \text{Na}_1\text{V}_2(\text{PO}_4)_3 > \text{Na}_1\text{Cr}_2(\text{PO}_4)_3$,²⁴ reflecting an identical trend in D_j values observed (see Figure 3a). Furthermore, the polyhedral volumes of transition-metal octahedra are $\sim 9.80 \text{ \AA}^3$ for TiO_6 , $\sim 9.33 \text{ \AA}^3$ for VO_6 , and $\sim 8.77 \text{ \AA}^3$ for CrO_6 . The bond distance between the migrating Na^+ at the transition state and nearby O^{2-} (which is linearly correlated with the migration barriers) follows a sequence of $\text{Na}_1\text{Ti}_2(\text{PO}_4)_3 (\sim 2.36 \text{ \AA}) >$

$\text{Na}_1\text{V}_2(\text{PO}_4)_3$ (~ 2.30 Å) $>$ $\text{Na}_1\text{Cr}_2(\text{PO}_4)_3$ (~ 2.27 Å). This sequence indicates the narrower sizes of the migration “bottleneck” from $\text{Na}_1\text{Ti}_2(\text{PO}_4)_3$, via $\text{Na}_1\text{V}_2(\text{PO}_4)_3$, to $\text{Na}_1\text{Cr}_2(\text{PO}_4)_3$, hence explaining the reduced values of D_j in Figure 3a.

The impact of transition metal ionic radii is lower at a higher Na content (i.e., at $x \sim 3$), since the large ionic radius of Na^+ (when six-coordinated) dictates lattice parameters more significantly. Thus, variations observed in E_{barrier} and D_j are to be linked to the electronic structure (and LFSE) of the transition metals involved than to changes in lattice parameters or bottleneck sizes. Specifically, LFSE stabilizes Cr^{III} ($3d^3$) more than V^{III} ($3d^2$; see Supporting Figure 8 in the SI), due to the high stability of the half-filled high-spin t_{2g} orbitals of Cr^{III} .¹⁰ A higher Na^+ E_{barrier} in $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3$ compared to $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ is expected as more energy is required to oxidize a Cr^{III} that is near a migrating Na^+ to Cr^{IV} , which is consistent with a lower value of D_j (Figure 3a) for $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3$ than that for $\text{Na}_3\text{V}_2(\text{PO}_4)_3$.

In the case of $\text{Na}_3\text{Ti}_2(\text{PO}_4)_3$, Na^+ migration is penalized compared to $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ since the highly stable configuration of Ti^{IV} ($3d^0$) needs to be reduced by the migrating Na^+ to the unpreferred Ti^{III} ($3d^1$) configuration. Thus, the energy cost associated with a local Ti reduction near a migrating Na causes the D_j for $\text{Na}_3\text{Ti}_2(\text{PO}_4)_3$ to be lower than $\text{Na}_3\text{V}_2(\text{PO}_4)_3$. In general, at composition $x > 2$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ shows consistently higher D_j compared to $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$ and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ (Figure 3a).

Extracting the Last Na from $\text{Na}_1\text{M}_2(\text{PO}_4)_3$. From the occupation of Na sites (Figure 3b) at $x = 1$, we identified that only Na(1) sites were fully occupied, whereas Na(2) sites were empty. Such an arrangement of the Na ions relates to the “structural integrity” of $\text{Na}_1\text{M}_2(\text{PO}_4)_3$, where only Na(1) is occupied and screens the electrostatic repulsions of nearby MO_6 octahedra stacked along the c axis imparting stability to the $\text{Na}_1\text{M}_2(\text{PO}_4)_3$.^{24,54–56} Furthermore, we observed a large site energy difference (~ 880 meV) between the lower energy Na(1) site and Na(2) at $x \sim 1$ in $\text{Na}_1\text{V}_2(\text{PO}_4)_3$ (see Supporting Figure 2 of the SI). These results indicate that Na(2) sites are thermodynamically unstable at $x \sim 1$, which hinders the ion transport in $\text{Na}_1\text{M}_2(\text{PO}_4)_3$.⁸ We also observed an abrupt decline of D_j (i.e., $\sim 5.8 \times 10^{-15}$ cm² s⁻¹) in $\text{Na}_1\text{V}_2(\text{PO}_4)_3$, suggesting that further Na extraction $x < 1$ is impractical. Such a drop of diffusivity at $x = 1$ has also been commented on in prior reports.^{38,49,50,57}

Low values of D_j at low Na concentrations limit the full utilization of NaSICON capacities. The extraction of the last Na-ion should happen via $\text{Na}_1\text{V}^{\text{IV}}\text{V}^{\text{IV}}(\text{PO}_4)_3 \leftrightarrow \text{V}^{\text{V}}\text{V}^{\text{IV}}(\text{PO}_4)_3 + e^- + \text{Na}^+$, in the case of $\text{Na}_x\text{V}_2(\text{PO}_4)_3$. This reaction is not redox-limited, as the high-voltage $\text{V}^{\text{V}}/\text{V}^{\text{IV}}$ redox couple is reversibly accessible.^{19,38,59} To date, the chemical Na extraction from $\text{Na}_1\text{V}_2(\text{PO}_4)_3$ has been elusive.²⁷ The impractical extraction from $\text{Na}_1\text{V}_2(\text{PO}_4)_3$ can be partially attributed to the low Na diffusivities (Figures 2 and 3).^{38,49,50}

We propose that atomic substitutions on either Na sites, transition metal sites, or the inclusion of alternative polyanion groups may represent practical approaches to facilitate the extraction of the last Na ion in these NaSICONs. The feasibility of such a method has been confirmed in several studies.^{19,55,60,61} The last Na ion can be extracted from $\text{Na}_1\text{Nb}_2(\text{PO}_4)_3$ forming the mix-valence $\text{Nb}_2(\text{PO}_4)_3$,⁶² or from the mixed NaSICON $\text{Na}_x\text{TiNb}(\text{PO}_4)_3$.^{63,64} Thus, mixing V with “softer” transition metals from the second and third rows,

bearing redox characteristics similar to those of vanadium, may unlock additional capacity in NaSICONs.

Migration Barriers in Mixed-Transition-Metal NaSICONs. On the one hand, at low Na content (i.e., $x = 1$) transition metals with higher oxidation states will tend to repel the Na ions at Na(1) electrostatically and hence destabilize the Na(1) site with an increase of the site energy at Na(1). In addition, the occurrence of transition metals with higher oxidation states will decrease the electron density on the surrounding O^{2-} , which will reduce their electrostatic attraction to Na ions and increase the repulsion between nearby “ O_3 ” faces of the MO_6 octahedra. This will contribute to enlarging the Na-migration bottlenecks.²⁴ On the other hand, transition metals with a lower oxidation state will attract more Na ions around, resulting in the population of nearby Na(2) sites, which may lower the site energy difference between Na(1) and Na(2) sites at the composition $x = 1$. These considerations suggest that the local charge arrangement with higher/lower oxidation states of transition metals may introduce disorder on the Na vacancy lattice, which may decrease the E_{barrier} at $x = 1$. To quantify this aspect, we evaluated additional Na-migration barriers for NaSICONs with mixed transition metals in a 1:1 ratio (see Figure 4).

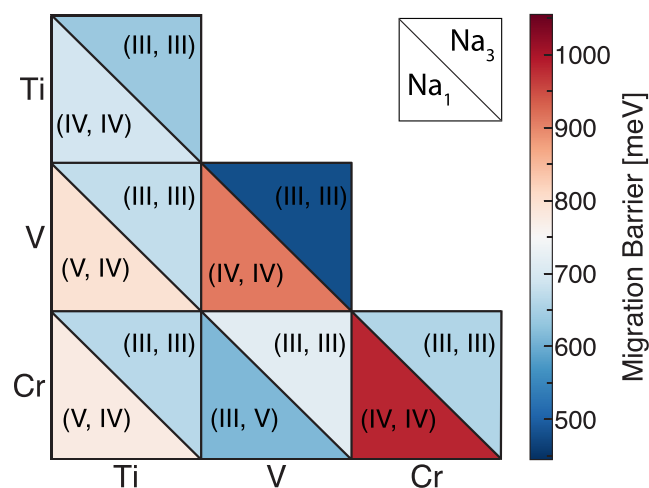


Figure 4. Migration barriers for $\text{Na}_1\text{MM}'(\text{PO}_4)_3$ and $\text{Na}_1\text{MM}'(\text{PO}_4)_3$, where M and M' = Ti, V, or Cr mixed transition metals, where M, M' = Ti, V, or Cr. The ratio of the transition metals is kept at 1:1. The three diagonal squares are 1-transition-metal NaSICONs, where only consistent tetra-valent (IV) and trivalent (III) states were observed at Na₁ and Na₃ compositions. Each square is divided into a lower triangle and a higher triangle, corresponding to the migration barriers for Na₁ and Na₃ compositions, respectively. Within each triangle, we identify the oxidation states of the two transition metals, which provide the local charge ordering environment for migrating Na^+ as (m, n), where m and n correspond to the oxidation states of the transition metal labeled on the y axis and x axis, respectively. For example, (III, V) in the lower-triangle of the $\text{Na}_1\text{CrV}(\text{PO}_4)_3$ square identifies the local charge arrangement of Cr^{III} and V^{V} oxidation states.

In $\text{Na}_1\text{VTi}(\text{PO}_4)_3$ and $\text{Na}_1\text{VCr}(\text{PO}_4)_3$, we observed an E_{barrier} of ~ 794 and ~ 613 meV, respectively (see Supporting Figure 10 in the SI), lower than the ~ 910 meV in $\text{Na}_1\text{V}_2(\text{PO}_4)_3$. Instead of the single oxidation state of V^{IV} observed at $\text{Na}_1\text{V}_2(\text{PO}_4)_3$, we found a local charge arrangement of V^{V} and Ti^{IV} redox states near the migrating Na ion in

$\text{Na}_1\text{VTi}(\text{PO}_4)_3$. Similarly, in $\text{Na}_1\text{VCr}(\text{PO}_4)_3$, suggest an ordering of the V^{V} and Cr^{III} states (see Supporting Figure 9 in the SI) in agreement with existing experiments.^{55,65} Furthermore, the site energy difference between Na(2) and Na(1) also decreased from ~ 880 meV for $\text{Na}_1\text{V}_2(\text{PO}_4)_3$ to 744 meV for $\text{Na}_1\text{VTi}(\text{PO}_4)_3$ and from 576 meV for $\text{Na}_1\text{VCr}(\text{PO}_4)_3$.

The lower values of E_{barrier} for mixed transition-metal NaSICONs at $x = 1$ will increase D_j for $\text{Na}_1\text{VTi}(\text{PO}_4)_3$ and $\text{Na}_1\text{VCr}(\text{PO}_4)_3$ by ~ 2 and ~ 4 orders of magnitude, respectively,⁴⁵ in comparison to a D_j of $\text{Na}_1\text{V}_2(\text{PO}_4)_3$. A lower E_{barrier} of 774 meV for $\text{Na}_1\text{TiCr}(\text{PO}_4)_3$ will also increase its D_j by approximately 3 orders of magnitude compared to $\text{Na}_1\text{Cr}_2(\text{PO}_4)_3$.

In $\text{Na}_3\text{VTi}(\text{PO}_4)_3$, $\text{Na}_3\text{VCr}(\text{PO}_4)_3$, and $\text{Na}_3\text{TiCr}(\text{PO}_4)_3$, the E_{barrier} values are ~ 676 meV, ~ 719 meV, and ~ 667 meV, respectively (see Supporting Figure 12 in the SI). Only trivalent transition metals, such as V^{III} , Ti^{III} , and Cr^{III} , were found in these systems (see Supporting Figure 11 in the SI), which set specific local charge arrangements for the migrating Na^+ . Compared with the migration barriers for the $\text{Na}_3\text{V}_2(\text{PO}_4)_3$, $\text{Na}_3\text{Ti}_2(\text{PO}_4)_3$, and $\text{Na}_3\text{Cr}_2(\text{PO}_4)_3$ NaSICON analogs at $x = 3$, which were ~ 485 , ~ 638 , and ~ 659 meV, respectively, the deviations between the E_{barrier} of single-transition-metal NaSICON and mixed-transition-metal NaSICON are as small as ~ 50 meV, except $\text{Na}_3\text{V}_2(\text{PO}_4)_3$, which exhibits a significantly lower E_{barrier} .

Our results in Figure 4 indicate that the local charge arrangements on the transition metal sites with higher/lower oxidation states may disrupt potentially stable Na–Va arrangements at $\text{Na}_1\text{M}_2(\text{PO}_4)_3$, thus lowering the migration barriers and enhancing the Na^+ D_j , which, in turn, may enable the extraction of the last Na. For example, in the case of the $\text{Na}_x\text{V}_2(\text{PO}_4)_3$ system, if compositions with low Na content (i.e., $\text{Na}_{0+x}\text{V}_2(\text{PO}_4)_3$) were thermodynamically stable, the Na extraction from $\text{Na}_1\text{V}_2(\text{PO}_4)_3$ would be highly facilitated because of the favorable local charge arrangement of the mixed-valence vanadium sites $\text{V}^{\text{IV/V}}$.

4. CONCLUSION

In conclusion, our *ab initio*-based kMC approach revealed the complex relationships among Na-ion transport in $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ NaSICON electrode materials as a function of Na content and temperatures. We identified optimal compositions providing maximum intrinsic Na^+ diffusivity for $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$. Our analysis demonstrated that the Na transport properties of NaSICON materials are highly dependent on the local chemical environments determined by the local arrangements of sodium ions and their vacancies as well as the oxidation states of transition metals. In particular, we elucidated that the environments favoring stable Na-vacancy orderings, typically in the fully charged region, should be disrupted to increase the energy density of NaSICON electrodes, such as $\text{Na}_x\text{V}_2(\text{PO}_4)_3$. The insights gained from this study into the Na^+ diffusion properties in $\text{Na}_x\text{Ti}_2(\text{PO}_4)_3$, $\text{Na}_x\text{V}_2(\text{PO}_4)_3$, and $\text{Na}_x\text{Cr}_2(\text{PO}_4)_3$ shed light on appropriately tailored combinations of transition metals that can be used to access swift Na transport in polyanionic electrodes for inexpensive Na-ion batteries.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsmaterialslett.3c00610>.

Details of simulations of migration barriers with first-principles methods, the formalism of the local cluster expansion, and details of kinetic Monte Carlo simulations (PDF)

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Notes

The authors declare no competing financial interest.

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