

# SENSITIVE ANALYSIS OF SOIL PARAMETERS ON STABILITY NUMBERS

*Bimlesh Kumar*

Research Scholar, Department of Civil Engineering, Indian Institute of Science, Bangalore - 560012, India  
bimk@civil.iisc.ernet.in

*Pijush Samui*

Research Scholar, Department of Civil Engineering, Indian Institute of Science, Bangalore -560012, India.  
pijush@civil.iisc.ernet.in

## Abstract

In general, Stability number can be expressed as a function comprising of pore water pressures coefficient ( $r_u$ ), horizontal earthquake coefficient ( $k_h$ ), slope angle ( $\beta$ ) and friction angle ( $\phi$ ) in associated flow rule. Then it is important to know how different parameters influence the stability number. These influences may be obtained through the sensitivity analysis of the parameters. Due its facility in solving non linear problems, Artificial Neural Networks (ANN) has been proposed, as a powerful tool, to represent the stability number. Neural Networks are typically thought of as black boxes trained to a specific task on a large number of data samples. In many applications it becomes necessary to “look inside” of these black boxes before they can be used in practice. Sensitivity analysis is one of best ways to look inside the neural model and ascertain that which parameters are having more effect on the output. Sensitivity analysis is a method for extracting the cause and effect relationship between the inputs and outputs of the network. The basic idea is that each input channel to the network is offset slightly and the corresponding change in the output(s) is reported. So, through differentiation of a previously trained net, the sensitivity factors of the main parameters of solar collectors is calculated and discussed. The sensitivity factors show how much the input variables influence the output variables. In this paper, the sensitivity analysis for stability number's main parameters is discussed. The result indicates that the  $r_u$  is having more influence on stability number than any other parameter followed by  $\beta$ ,  $k_h$  and  $\phi$ . The stability numbers have been found to decrease continuously with (i) increase in  $r_u$ , (ii) increase in  $k_h$  and (iii) increase in slope angle ( $\beta$ ) (iv) decrease in  $\phi$ .

*Key words: slope stability, Artificial Neural Network, stability number.*

## INTRODUCTION

The stability of homogeneous slopes can be expressed in terms of a dimensionless group known as the stability number,  $N$ , which is defined as,  $\gamma H_c/c$  where ‘ $c$ ’ is the cohesion,  $\gamma$  is the bulk unit weight of the soil and  $H_c$  is critical height of the slope. The design of earthen embankments is quite often carried out with the use of stability numbers as originally introduced by Taylor (1948). Taylor provided the charts indicating the variation of  $N_s$  for homogeneous slope with changes in slope angle ( $\beta$ ) for various soil friction angles ( $\phi$ ). Later on Bishop (1955) used the method of slices in obtaining the stability of slopes. In order to solve the problem, Bishop assumed that the resultant of inter slices forces acts in the horizontal direction. It is found that the method of slice do not satisfy all the conditions of statical equilibrium. Chen (1975) used the upper bound theorem of the limit analysis to obtain the critical heights for the homogeneous soil slopes. A rotational discontinuity mechanism was assumed in this analysis; it was indicated that in order that the rupture surface remains kinematically admissible, its shape should become an arc of the logarithmic spiral. However, Chen (1975) did not incorporate either the effect of pseudo-static earthquake body forces or the pore water pressure. Michalowski (2002) also used the upper bound theorem of limit analysis in order to obtain the stability numbers for homogeneous slopes in the presence of pore water pressures as well as pseudo-static earthquake forces and formulated the following expression;



## SENSITIVITY ANALYSIS

Sensitivity analysis is a method for extracting the cause and effect relationship between the inputs and outputs of the network. The basic idea is that each input channel to the network is offset slightly and the corresponding change in the output is reported. To ascertain the influence of the input variables on output variables, sensitivity analysis is also carried out. This testing process provides a measure of the relative importance among the inputs of the neural model and illustrates how the model output varies in response to variation of an input. The first input is varied between its mean  $\pm$  standard deviations while all other inputs are fixed at their respective means. Similar exercises have been made for all others input parameters.

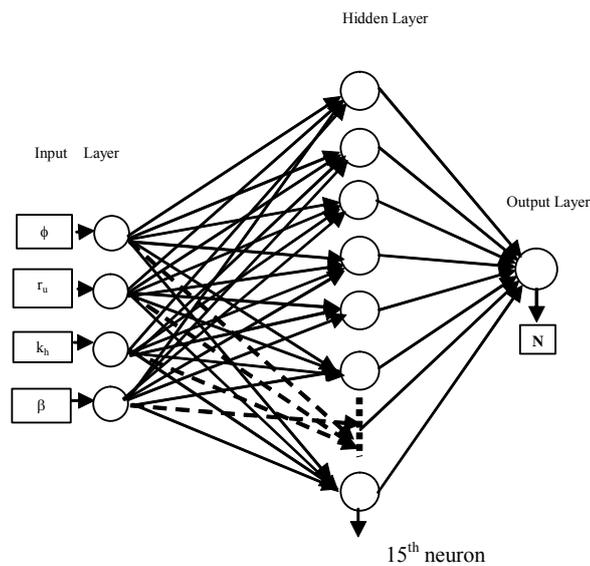


Figure 2. Neural net architecture used in the analysis.

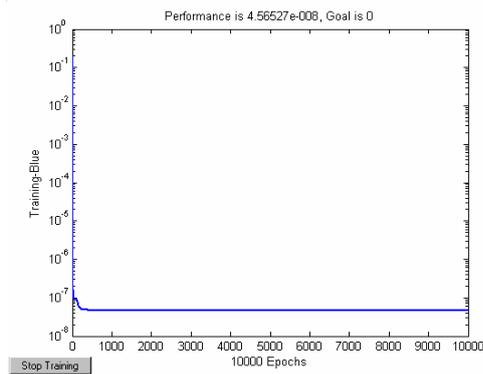


Figure3. MSE versus epochs.

As shown in Figure 6, pore water pressure coefficient is having more influence on stability number followed by the slope angle ( $\beta$ ),  $k_h$  and  $\phi$ . The stability number as a function of  $r_u$  by keeping the other parameters as constant, as predicted by the ANN model is shown in Figure 7. The stability numbers have been found to decrease with an increase in  $r_u$ . Figure 8 gives the stability numbers characteristics as a function of  $k_h$ . It has been found that the stability numbers is decreasing

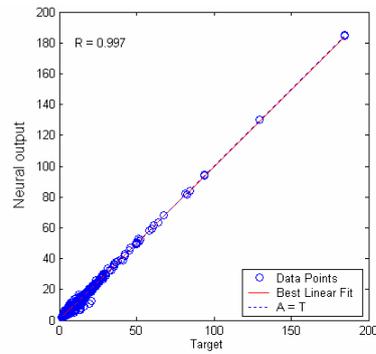


Figure 4. Results of training phase.

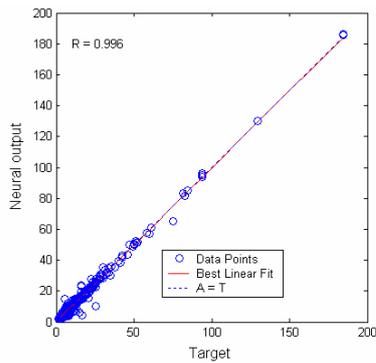


Figure 5. Results of testing phase.

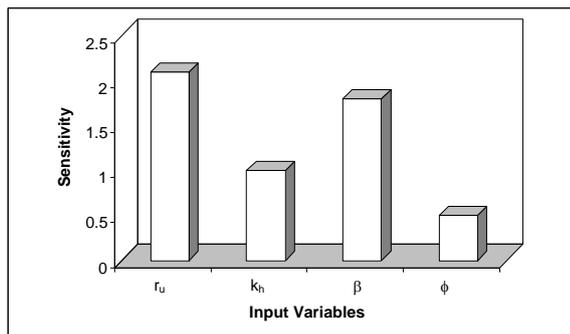
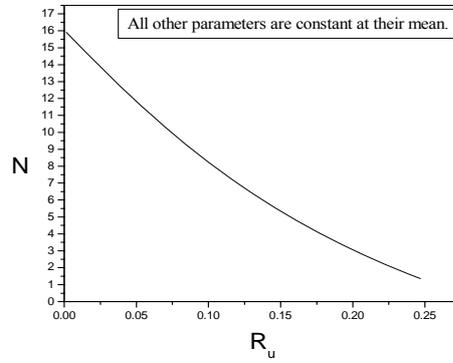
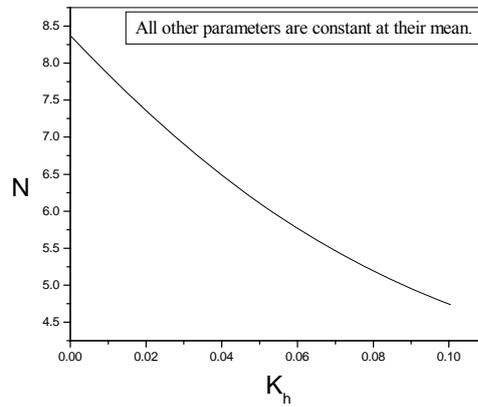


Figure 6. Sensitivity analysis of Stability numbers.

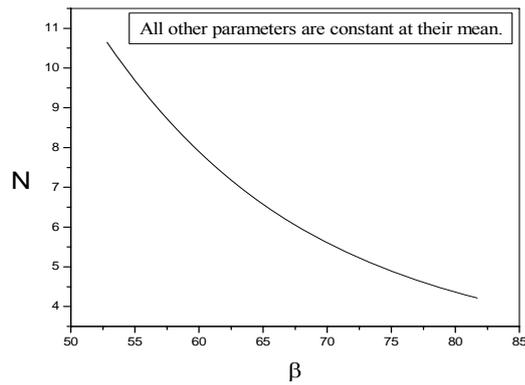
with an increase in  $k_h$ . Effect of slope angle is illustrated in Figure 9. It shows that the stability numbers have been found to decrease continuously with an increase in slope angle  $\beta$ . Effect of friction angle  $\phi$  is depicted in Figure 10. It is seen clearly from Figure 10 that an increase in  $\phi$  will increase the stability number.



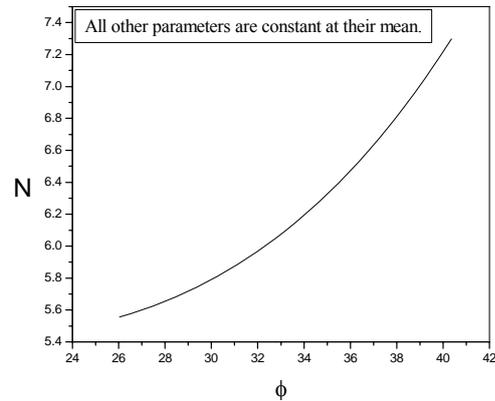
**Figure 7. Effect of  $r_u$  on stability number.**



**Figure 8. Effect of  $k_h$  on stability number.**



**Figure 9. Effect of  $\beta$  on stability number.**



**Figure 10. Effect of  $\phi$  on stability number.**

## CONCLUSION

The results presented in this paper have clearly shown that the neural network methodology can be used efficiently to predict the stability numbers for non homogeneous soil slope. The main advantage of neural networks is to remove the burden of finding an appropriate model structure or to find a useful regression equation. The network showed excellent learning performance and achieved good generalization. Sensitivity analyses with the trained neural net or during training could provide valuable additional information on the relative influence of various parameters on the stability number. The  $r_u$  is having more influence on stability number than any other parameter. The stability numbers have been found to decrease continuously with (i) increase in  $r_u$ , (ii) increase in  $k_h$  and (iii) increase in slope angle ( $\beta$ ). The stability number will increase with an increase in  $\phi$ .

## REFERENCES

- Bishop, A.W. (1955). The use of slip circle in the stability of slopes, *Geotechnique*, Vol. 5(1), pp 7-17.
- Chen, W.F. (1975). *Limit analysis and soil plasticity*. Elsevier, Amsterdam.
- McCulloch, W.S. and Pitts, W. (1943). A logical calculus in the ideas immanent in nervous activity, *Bull. Math.Biophys*, Vol. 5, pp 115-133.
- Michalowski, R.L. (2002). Stability charts for uniform slopes, *Journal of Geotechnical and Geoenvironmental Engineering*, ASCE, Vol. 128(4), pp 351-355.
- More, J.J. (1977). The Levenberg-Marquardt algorithm: Implementation and theory. Heidelberg: Springer, *Numerical Analysis*, Watson, G.A., ed., 105-116.
- Taylor, D.W. (1948). *Fundamental of soil mechanics*. John Wiley, New York.