# Novel and Polynuclear K- and Na-Based Superalkali Hydroxides as Superbases Better than Li-Related Species and Their Enhanced Properties: From ab Initio Exploration 

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Table S1. Natural Charges and O-H Stretching Frequencies of the Neutral Superalkali $\mathrm{XM}_{\mathrm{n}+1} \mathrm{OH}$ and $\mathrm{XM}_{\mathrm{n}+1} \mathrm{OH}_{2}{ }^{+}$Species Using MP2/6-311++G(d, p) Level of Theory

| Species | Natural Charge (Q) (in e) |  |  |  |  | $\mathrm{O}-\mathrm{H}$(stretching)$\left(\right.$ in cm $^{-1}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M (ring) | Qo of O-H | Qн of O-H | Qx | Qm (terminal) |  |
| KOH | 0.985 | -1.413 | 0.428 | - | - | 3961.4 |
| $\mathrm{KOH}_{2}{ }^{+}$ | 0.998 | -0.972 | 0.486 | - | - | $\begin{aligned} & \text { sym: } 3854.3 \\ & \text { asym: } 3946.8 \end{aligned}$ |
| $\mathrm{FK}_{2} \mathrm{OH}$ | 0.976 | -1.402 | 0.423 | $\mathrm{F}(-0.973)$ | - | 3934.4 |
| $\mathrm{FK}_{2} \mathrm{OH}_{2}{ }^{+}$ | 0.988 | -0.933 | 0.468 | F (-0.979) | - | sym: 3848.2 asym: 3949.8 |
| $\mathrm{OK}_{3} \mathrm{OH}$ | 0.955 | -1.389 | 0.416 | O (-1.89) | 0.952 | 3934 |
| $\mathrm{OK}_{3} \mathrm{OH}_{2}{ }^{+}$ | 0.958 | -0.938 | 0.471 | O (-1.883) | 0.963 | sym: 3849.6 <br> asym: 3950.9 |
| $\mathrm{NK}_{4} \mathrm{OH}$ | 0.903 | -1.388 | 0.397 | N (-3.675) | 0.884 | 3940 |
| $\mathrm{NK}_{4} \mathrm{OH}_{2}{ }^{+}$ | 0.872 | -0.94 | 0.471 | $\mathrm{N}(-2.424)$ | 0.839 | $\begin{aligned} & \text { sym: } 3833.6 \\ & \text { asym: } 3939.2 \\ & \hline \end{aligned}$ |
| NaOH | 0.984 | -1.419 | 0.436 | - | - | 4012.5 |
| $\mathrm{NaOH}_{2}{ }^{+}$ | 0.993 | -0.986 | 0.496 | - | - | $\begin{aligned} & \text { sym: } 3855.3 \\ & \text { asym: } 3945.4 \\ & \hline \end{aligned}$ |
| $\mathrm{FNa}_{2} \mathrm{OH}$ | 0.967 | -1.403 | 0.435 | F (-0.967) | - | 3969.8 |
| $\mathrm{FNa}_{2} \mathrm{OH}_{2}{ }^{+}$ | 0.969 | -0.95 | 0.478 | F (-0.945) | - | $\begin{aligned} & \text { sym: } 3833 \\ & \text { asym: } 3927.2 \\ & \hline \end{aligned}$ |
| $\mathrm{ONa}_{3} \mathrm{OH}$ | 0.947 | -1.383 | 0.428 | O (-1.903) | 0.964 | 3967 |
| $\mathrm{ONa}_{3} \mathrm{OH}_{2}{ }^{+}$ | 0.956 | -0.941 | 0.48 | O (-1.902) | 0.97 | $\begin{aligned} & \text { sym: } 3876.8 \\ & \text { asym: } 3926.3 \\ & \hline \end{aligned}$ |
| $\mathrm{NNa4} \mathrm{OH}$ | 0.927 | -1.369 | 0.425 | $\mathrm{N}(-2.55)$ | 0.821 | 3958 |
| $\mathrm{NNa}_{4} \mathrm{OH}_{2}{ }^{+}$ | 0.901 | -0.936 | 0.479 | N (-2.582) | 0.879 | $\begin{gathered} \text { sym: } 3881.7 \\ \text { asym: } 3918.2 \\ \hline \end{gathered}$ |
| LiOH | 0.96 | -1.407 | 0.445 | - | - | 4049.8 |
| $\mathrm{LiOH}_{2}{ }^{+}$ | 0.99 | (-1.016 | 0.513 | - | - | $\begin{aligned} & \text { sym: } 3833.3 \\ & \text { asym: } 3918.4 \end{aligned}$ |
| $\mathrm{FLi}_{2} \mathrm{OH}$ | 0.91 | -1.368 | 0.459 | $\mathrm{F}(-0.912)$ | - | 4016.8 |
| $\mathrm{FLi}_{2} \mathrm{OH}_{2}{ }^{+}$ | 0.974 | (-0.984 | 0.497 | F (-0.959) | - | sym: 3803.7 <br> asym: 3892.5 |
| $\mathrm{OLi}_{3} \mathrm{OH}$ | 0.871 | -1.34 | 0.45 | O (-1.767) | 0.915 | 4009.2 |
| $\mathrm{OLi}_{3} \mathrm{OH}_{2}{ }^{+}$ | 0.949 | (-0.972 | 0.495 | O (-1.886) | 0.969 | sym: 3811.1 <br> asym: 3905.7 |
| $\mathrm{NLi}_{4} \mathrm{OH}$ | 0.817 | -1.317 | 0.448 | $\mathrm{N}(-2.454)$ | 0.845 | 3996 |
| $\mathrm{NLi4}_{4} \mathrm{OH}_{2}{ }^{+}$ | 0.915 | (-0.963 | 0.493 | $\mathrm{N}(-2.723)$ | 0.935 | sym: 3805.1 <br> asym: 3904.9 |

Table S2. O-M bond lengths and changes therein (non-protonated to protonated SAHs)
O-K distance
$\mathrm{KOH}(2.244)$ to $\mathrm{KOH}_{2}{ }^{+}$(2.629) (change in O-K: 0.385)
$\mathrm{FK}_{2} \mathrm{OH}(2.476)$ to $\mathrm{FK}_{2} \mathrm{OH}_{2}{ }^{+}$(3.241) (change in $\mathrm{O}-\mathrm{K}: 0.765$ )
$\mathrm{OK}_{3} \mathrm{OH}$ (2.497) to $\mathrm{OK}_{3} \mathrm{OH}_{2}{ }^{+}$(3.008) (change in $\mathrm{O}-\mathrm{K}: ~ 0.511$ )
$\mathrm{NK}_{4} \mathrm{OH}(2.446)$ to $\mathrm{NK}_{4} \mathrm{OH}_{2}{ }^{+}(3.007)$ (change in O-K: 0.561 )
O-Na distance
NaOH (1.98) to $\mathrm{NaOH}_{2}{ }^{+}$(2.27) (change in O-Na: 0.29)
$\mathrm{FNa}_{2} \mathrm{OH}(2.165)$ to $\mathrm{FNa}_{2} \mathrm{OH}_{2}{ }^{+}(2.792)$ (change in $\mathrm{O}-\mathrm{Na}: 0.627$ )
$\mathrm{ONa}_{3} \mathrm{OH}(2.181)$ to $\mathrm{ONa}_{3} \mathrm{OH}_{2}{ }^{+}$(2.696) (change in O-Na: 0.515)
$\mathrm{NNa}_{4} \mathrm{OH}$ (2.167) to $\mathrm{NNa}_{4} \mathrm{OH}_{2}{ }^{+}$(2.722) (change in O-Na: 0.555)

O-Li distance
LiOH (1.607) to $\mathrm{LiOH}_{2}{ }^{+}$(1.869) (change in O-Na: 0.262)
$\mathrm{FLi}_{2} \mathrm{OH}(1.796)$ to $\mathrm{FLi}_{2} \mathrm{OH}_{2}{ }^{+}(2.296)$ (change in $\mathrm{O}-\mathrm{Na}: 0.5$ )
$\mathrm{OLi}_{3} \mathrm{OH}$ (1.81) to $\mathrm{OLi}_{3} \mathrm{OH}_{2}{ }^{+}$(2.217) (change in $\mathrm{O}-\mathrm{Na}: 0.407$ )
$\mathrm{NLi}_{4} \mathrm{OH}(1.812)$ to $\mathrm{NLi}_{4} \mathrm{OH}_{2}{ }^{+}$(2.217) (change in O-Na: 0.405)

## Cartesian Coordinates at MP2/6-311++G(d, p) Level of Theory Superalkalis Neutral Species

## $\mathrm{FK}_{2}$

F,0,-2.0764656765,-0.1082196994,0.
K,0,0.2670339483,-0.2561589919,0.
K,0,-2.9981956415,2.0514771305,0.
$\mathrm{OK}_{3}$
O,0,0.0000090301,-0.0000080754,-0.0000182145
K,0,-0.2022693064,2.3587166159,0.0000093387
K,0,2.1438736777,-1.0041740819,0.0000093383
K,0,-1.9415634015,-1.3545424587,-0.0000214624

NK4
N,0,0.,0.,0.0000066066
K,0,0.,2.1125288733,1.4937574538
K,0,0.,-2.1125288733,1.4937574538
K,0,-2.1125290231,0.,-1.4937478439
K,0,2.1125290231,0.,-1.4937478439

FNa 2
F,0,-2.2581877248,-0.3653504506,0.
Na,0,-0.1497973055,-0.2140321682,0.
Na,0,-2.8193440199,1.672616918,0.
$\mathrm{ONa}_{3}$
O,0,-0.0000543243,-0.0002367844,-0.0000237437
$\mathrm{Na}, 0,0.1501268851,2.0900010143,-0.0000056952$
Na,0,-1.8854997662,-0.9149636286,-0.0000176159
Na,0,1.7352862054,-1.1748836013,0.0000380548

## NNa4 at MP2/6-31+G(d, $\mathbf{p}$ ) level

N,0,0.00000646,-0.0000008046,-0.0000133593
Na,0,-0.9276286111,-1.7748495387,-0.8434563834
$\mathrm{Na}, 0,-0.9310330587,1.7736707088,-0.8421809048$
$\mathrm{Na}, 0,-0.2625920396,-0.0010263633,2.1570699563$
$\mathrm{Na}, 0,2.1212662495,0.0022059979,-0.4714593089$

NNa4 (TS = -693.6 cm ${ }^{-1}$ ) Using MP2/6-311++G(d, p) Level of Theory
N,0,0.,0.,-0.0049359312
K,0,0.,1.9270027821,-1.62993159
K,0,0.,-1.9270027821,-1.62993159
K,0,1.9268202371,0.,1.6202183484
K,0,-1.9268202371,0.,1.6202183484

## FLi 2

F,0,-2.1941574243,-0.2747496747,0.
Li,0,-2.652535367,1.3666576348,0.
Li,0,-0.4938890901,-0.1589227099,0.
$\mathrm{OLi}_{3}$
O,0,0.0000062325,0.0001011064,-0.00000231
Li,0,-1.4429352766,0.9101647345,0.0000017698
Li,0,1.5097399588,0.7944542793,0.0000017699
Li,0,-0.0668259147,-1.7046031202,0.0000017703
$\mathrm{NLi}_{4}$
N,0,-0.000005661,0.0000061737,-0.0000174447
Li,0,0.2813964864,-0.6859791493,1.6015659878
Li,0,-0.3876710919,1.714845645,0.1543628591
Li,0,-1.3465037603,-0.8404122764,-0.7716613204
Li,0,1.4527950267,-0.1884343929,-0.9842210817

## Superalkali Hydroxides (SAHs)

## KOH

O,0,0.,0.,-1.5063512941
H,0,0.,0.,-2.4637327596
K,0,0.,0.,0.7379280537
$\mathrm{FK}_{2} \mathrm{OH}$
F,0,-0.0000087131,1.645369891,0.0001409423
O,0,0.0000425974,-1.7159024166,0.0002706946
H,0,0.0000049972,-2.675132356,0.0002737398
$\mathrm{K}, 0,1.7625164738,0.0229894062,0.0003984298$
K,0,-1.7624863552,0.0229794755,0.0003991935

## $\mathrm{OK}_{3} \mathrm{OH}$

O,0,0.796487,0.000499,0.000109
O,0,-2.870855,-0.000854,-0.000113
H,0,-3.830036,0.000801,-0.000196
K,0,-1.014928,-1.670334,0.00003
K,0,-1.015587,1.6704,0.00003
K,0,3.105514,0.000042,-0.000049

## $\mathrm{NK}_{4} \mathrm{OH}$

N,0,0.,0.,-0.5806881781
О,0,0.,0.,3.1065767208
H,0,0.,0.,4.066035769
K,0,0.,1.8497691716,1.5055039046
K,0,0.,-1.8497691716,1.5055039046
K,0,-2.1818381595,0.,-2.1560255605
K,0,2.1818381595,0.,-2.1560255605

## NaOH

$\mathrm{Na}, 0,0 ., 0 ., 0.9373441018$
O,0,0.,0.,-1.0427745508
H,0,0.,0.,-1.9969085511

## $\mathrm{FNa}_{2} \mathrm{OH}$

F,0,1.6039327037,-0.0000412779,0.0000290978
O,0,-1.570102858,0.0000405166,-0.00006631873
Н, $0,-2.5271967673,0.0000767766,-0.0001012457$
$\mathrm{Na}, 0,0.022617518,1.4670816649,0.0000111675$
$\mathrm{Na}, 0,0.0225394037,-1.4670806802,0.0000111677$

## ONa 3 OH

O,0,-0.909175135,0.0046267942,0.0005067097
O,0,2.4559111495,-0.005555908,-0.0005126826
Н,0,3.4131885833,-0.0082026155,-0.0007151003
$\mathrm{Na}, 0,0.7676594817,-1.3857767726,0.0001174921$
Na,0,0.7758461606,1.3847762515,0.0001076261
Na,0,-2.9656652401,0.0019682504,0.0000449549

## NNa 4 OH

N,0,0.6671083436,0.0000276355,0.0001009931
O,0,-2.7200579928,-0.0001142913,-0.0001322223
H,0,-3.6781995071,-0.0001926228,-0.0001540436
$\mathrm{Na}, 0,2.0759571631,-1.7546397376,0.0000485271$
Na,0,2.0760873293,1.7545672935,0.0000331366
$\mathrm{Na}, 0,-1.1333548772,0.0000950177,-1.4758552496$
Na,0,-1.1335814588,0.000109705,1.4758318588

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## LiOH

O,0,0.,0.,0.3220964877
H,0,0.,0.,1.2740270981
Li,0,0.,0.,-1.2844745858
$\mathrm{FLi}_{2} \mathbf{O H}$
F, $0,-1.382927742,0.0001604723,0.0001481302$
Li,0,-0.064647964,-1.1460442691,-0.0001068386
Li,0,-0.0644304955,1.1461716565,-0.0001068514
O,0,1.3164022713,-0.0001053427,0.0000544151
H,0,2.2848429302,-0.0000395169,0.0002391448

## $\mathrm{OLi}_{3} \mathrm{OH}$

O,0,-1.1680681452,0.0002099513,0.00086669869
Li,0,0.2589991333,-1.0906514032,0.0000943842
Li,0,0.2593322938,1.0907823782,0.0000904251
Li,0,-2.8274047688,-0.0005527675,-0.0007480446
O,0,1.703205989,-0.0002235644,-0.0004117705
H,0,2.6576434978,-0.0003685944,0.0014350188

## NLi 4 OH

$\mathrm{N}, 0,-1.1193283489,0.0000258879,-0.0001263635$
Li,0,-2.1134311162,1.4902136228,-0.0003582347
Li,0,-2.1133805098,-1.4901978005,-0.0001938448
Li,0,0.4437233099,0.000070887,1.1093155499
Li,0,0.44400434,-0.0000482592,-1.109164358
O,0,1.8771834054,-0.0000283195,0.000233442
H,0,2.8324539196,0.0001139815,0.0004368091

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## Protonated Superalkali Hydroxides (PSAHs)

## $\mathrm{KOH}_{2}{ }^{+}$

O,0,0.2215546808,-0.2049669382,-1.4162244599
H,0,-0.458299532,-0.7701757514,-1.7979692695
K,0,0.8194860158,0.1463057342,1.1199391672
H,0,0.6264971247,0.2035300377,-2.18858686889
$\mathrm{FK}_{2} \mathrm{OH}_{2}{ }^{+}$(Linear)
O,0,-4.0295416725,-0.240958915,0.000001724
Н,0,-4.2649261088,-1.1734980617,0.0000130463
H,0,-4.8825596847,0.2033601231,-0.0000105191
F,0,0.7463529001,0.1442117035,0.0000036648
K,0,-1.532000545,0.8206714912,-0.0000186289
K,0,2.9958251109,-0.4791383411,0.0000127128
$\mathbf{F K}_{2} \mathrm{OH}_{2}{ }^{+}$(Ring)
F,0,0.0000055468,-1.1436325614,0.0000273358
O,0,-0.0000124284,2.0953141987,0.000205727
Н,0,-0.0000447699,2.6977699041,-0.7510436559
K,0,-2.1685771604,-0.3137332065,-0.0000705542
K,0,2.1685769411,-0.3137025191,-0.0000573672
H,0,-0.0000071292,2.6972061841,0.7519065145
$\mathrm{OK}_{3} \mathrm{OH}_{2}{ }^{+}$
O,0,0.677736956,0.0000823748,-0.0000963372
O,0,-3.0741296619,-0.0003235093,0.0002499455
Н,0,-3.6744885843,-0.0003835258,0.7530945162
K,0,-0.7441436051,-1.9022498208,0.0002299589
K,0,-0.7445436681,1.9021140361,0.0002296487
K,0,3.0437000119,0.0003183752,-0.0003366301
H,0,-3.6744744486,-0.0003839301,-0.7526061019

## $\mathrm{NK}_{4} \mathrm{OH}_{2}{ }^{+}$

N,0,0.,0.,-0.5036402793
O,0,0.,0.,3.419026882
H,0,0.,0.7536908691,4.0195521882
K,0,-1.9733733513,0.,1.1507024181
K,0,1.9733733513,0.,1.1507024181
K,0,0.,-2.1020287421,-2.0289119077
K,0,0.,2.1020287421,-2.0289119077
H,0,0.,-0.7536908691,4.0195521882

## $\mathrm{NaOH}_{2}{ }^{+}$

$\mathrm{Na}, 0,-0.000010412,-1.1375000114,0$.
O,0,0.0000094162,1.132209436,0.
H,0,0.0000584979,1.7245952875,0.7594271047
H,0,0.0000584979,1.7245952875,-0.7594271047
$\mathbf{F N a}_{2} \mathrm{OH}_{2}{ }^{+}$(Linear)
O,0,-2.0334973875,0.0000217257,0.0000011311
H,0,-2.625867744,-0.7589516467,0.000003457
H,0,-2.6256626806,0.7591558221,0.00000035199
F,0,2.4253358882,0.0000706531,-0.0000004471
$\mathrm{Na}, 0,0.2971871634,-0.0000432207,-0.0000093783$
$\mathrm{Na}, 0,4.5021417606,-0.0000466836,0.0000074374$
$\mathrm{FNa}_{2} \mathrm{OH}_{2}{ }^{+}$(Ring)
F,0,0.0000000179,1.3037726124,0.0007272073
O,0,0.0000005344,-1.7650273649,0.0000523458
H,0,0.0000004139,-2.3678756172,0.7530206526
$\mathrm{Na}, 0,1.8353070084,0.3391331114,-0.0004960512$
$\mathrm{Na}, 0,-1.8353063885,0.3391319694,-0.0004960512$
H,0,0.000000414,-2.3682257112,-0.7526351034

## $\mathrm{ONa}_{3} \mathrm{OH}_{2}{ }^{+}$

O,0,0.,0.,0.82847
O,0,0.,0.,-2.648505
H,0,0.756075,0.,-3.248687
Na,0,0.,1.631893,-0.502435
Na,0,0.,-1.631893,-0.502435
Na,0,0.,0.,2.919202
H,0,-0.756075,0.,-3.248687
$\mathrm{NNa}_{4} \mathrm{OH}_{2}{ }^{+}$
$\mathrm{N}, 0,0.6769547143,0.0000717761,-0.0000758719$
O,0,-2.9776302433,0.0002457965,0.000009627
H,0,-3.577866873,-0.7566934728,-0.0001244327
Na,0,2.0425504036,1.7785117755,0.0002811556
$\mathrm{Na}, 0,2.0433358348,-1.7777780269,-0.0009078794$
Na,0,-0.8271947816,-0.0007840666,1.6702114476
$\mathrm{Na}, 0,-0.8280757521,0.0003098852,-1.6696087856$
H,0,-3.5772163027,0.757699333,0.0003807393

## $\mathbf{L i O H}_{2}{ }^{+}$

O,0,0.2014078595,-0.2060429207,0.23658102
Н,0,-0.4309295619,-0.7457772947,0.7261926928
Li,0,0.4195319535,-0.1064341795,-1.616568104
H,0,0.6908241718,0.2771987543,0.9132142707

## $\mathbf{F L i}_{2} \mathbf{O H}_{2}{ }^{+}$(Linear)

O,0,-1.3398777368,-0.0000171599,0.0000501306
H,0,-1.9260828002,-0.0000227302,-0.7638188766
Н,0,-1.9257772624,-0.0000227337,0.7641560217
Li,0,0.5712634618,0.0000020807,0.0001143776
F,0,2.2911250242,0.0000020073,0.0002540727
Li,0,3.9720321734,0.0000019257,0.000342654

## $\mathbf{F L i}_{2} \mathrm{OH}_{2}{ }^{+}$(Ring)

F, $0,1.3774892875,-0.0000017106,-0.0000725026$
Li,0,0.4383847827,-1.4024845852,-0.0000579538
Li,0,0.4383948644,1.4024875141,-0.0000579539
O,0,-1.3796263113,0.0000006674,0.0000813161
Н,0,-1.9812755979,0.0000015571,-0.7567835729
Н,0,-1.9811090254,0.0000015572,0.7570786671

## $\mathrm{OLi}_{3} \mathrm{OH}_{2}{ }^{+}$

O,0,1.2176748224,0.0000024113,-0.0001032855
Li,0,0.0552213108,-1.2698973576,-0.0000478516
Li,0,0.0553623478,1.2700311067,-0.0000466875
Li,0,2.9200547354,-0.0001124767,-0.0001844617
O,0,-1.7613386472,0.000022435,0.0001150897
H,0,-2.3589229873,0.0000318112,-0.7589281374
H,0,-2.3587885819,0.0000310702,0.7592643339
$\mathrm{NLi}_{4} \mathrm{OH}_{2}{ }^{+}$
$\mathrm{N}, 0,1.1816451508,0.0000492699,-0.0001159297$
Li,0,2.2461167866,-1.4645957349,-0.000233468
Li,0,2.2459645428,1.4648054296,-0.0002744248
Li,0,-0.1454464454,-0.0000679855,1.2643068797
Li,0,-0.1457950341,-0.0000345145,-1.2641964804
O,0,-1.9671086859,-0.0000465064,0.0001878888
Н,0,-2.5637467002,-0.7599190401,0.0002394227
H,0,-2.5636226147,0.7599230818,0.0002571117

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