

660-km density jump), these forces are strong enough to produce partial layering in the mantle. The strength of the buoyancy forces, however, is proportional to the assumed density contrast across the interface. If the density contrast across the 660-km discontinuity is only 5%, as our results suggest, then layered convection is less likely.

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Improved Weather and Seasonal Climate Forecasts from Multimodel Superensemble

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A method for improving weather and climate forecast skill has been developed. It is called a superensemble, and it arose from a study of the statistical properties of a low-order spectral model. Multiple regression was used to determine coefficients from multimodel forecasts and observations. The coefficients were then used in the superensemble technique. The superensemble was shown to outperform all model forecasts for multiseasonal, medium-range weather and hurricane forecasts. In addition, the superensemble was shown to have higher skill than forecasts based solely on ensemble averaging.

Sophisticated numerical models used in operational and research centers throughout the globe routinely make short-term (1 to 7 days in advance) weather and seasonal (one to several seasons in advance) climate forecasts. Individually each modeling group tracks the forecast skill of their model. Within recent years, the use of model ensembles has become an important forecasting component. The methodology of how to generate the ensemble is the focus of many forecasting centers. Here we show that a multimodel

superensemble can more accurately predict weather and seasonal climate. The superensemble is developed by using a number of forecasts from a variety of weather and climate models. Along with the benchmark observed (analysis) fields, these forecasts are used to derive simple statistics on the past behavior of the models. These statistics, combined with multimodel forecasts, enable us to construct a superensemble forecast.

Given a set of past multimodel forecasts, we used a multiple regression technique (for the multimodels), in which the model forecasts were regressed against an observed (analysis) field. We then used least-squares minimization of the difference between the model and the analysis field to determine the

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weights. We carried out this minimization at all vertical levels, at all geographic locations (the grid points of the multimodels), and for all model variables.

The motivation for this approach came from construction of a multimodel superensemble from a low-order spectral model (1). In this low-order model, it is possible to introduce various (proxy) versions of cumulus parameterization (or model physics) by simply altering a forcing term. Time integration of this system showed that the multiple regression coefficients of these multimodels (regressed against the nature run) showed a marked time invariance. This time invariance is a key element for the success of the proposed method.

We used many models at various horizontal and vertical resolutions. Most of the models had a horizontal resolution of <250 km and a ver-

tical resolution of about 1 km. Model output was interpolated to a common grid of 2.5° and 100 hPa vertically. These global models include parameterizations of physical processes; effects of ocean, snow, and ice cover; and treatment of orography. We divided the run timeline into a control and a forecast part. The observed (or the analysis) fields are used only during the control period to determine the weights.

The Atmospheric Model Intercomparison Project (AMIP) data set (2) was used to test our procedure for seasonal forecasting. This data set contains a 10-year integration with 31 global atmospheric general circulation models, all beginning from a prescribed initial time of 1 January 1979 and subject to identical prescribed sea surface temperature (SST) and sea ice boundary forcings (3, 4). The control and forecast periods for the superensemble forecasts were arbitrarily derived from these 10-year-

long histories of eight selected models at two different timelines: Bureau of Meteorology Research Center (BMRC), Melbourne; Council of Scientific and Industrial Research Organization (CSIRO), Melbourne; European Center for Medium Range Weather Forecasts (ECMWF), London; Geophysical Fluid Dynamics Laboratory (GFDL), Princeton; Laboratory Meteorologic Dynamique (LMD), Paris; Max Planck Institute (MPI), Hamburg; National Center for Environmental Predictions (NCEP), Washington, D.C.; and United Kingdom Meteorological Office (UKMO), London. The first timeline, January 1981 through December 1988, was the control, and January 1979 through December 1980 was used for the forecast. The monthly means of the forecasts and the observed (analysis) fields of the past 8 years were used to generate the statistical weights. The most typical results for this timeline for the root-mean-square (rms) error of the south-north component of winds at 850 hPa (about 1.5 km over the ocean) averaged over an Asian monsoon domain bounded between 50°E and 120°E and between 30°S and 35°N are shown in Fig. 1A. The rms errors for the superensemble and its regression are comparable to typical analysis errors. Examination of the forecast period shows that the superensemble outperforms all models.

In the second timeline, the period January 1979 through December 1986 defines the control and January 1987 through December 1988 defines the forecast. A time history of precipitation forecast skill with the second

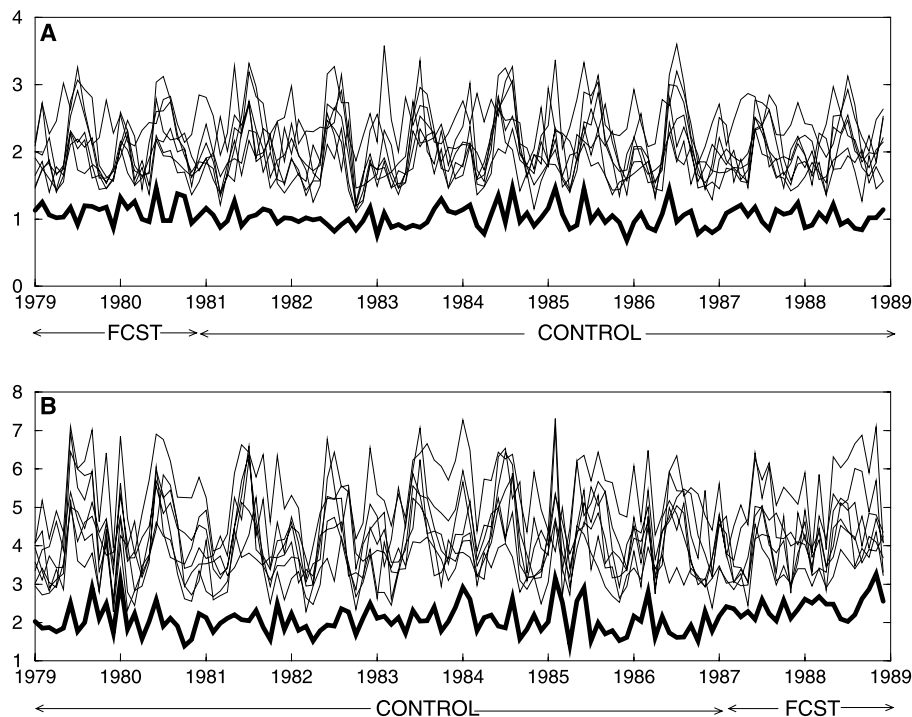


Fig. 1. Asian monsoon domain average rms error for the superensemble (heavy line) and the selected AMIP models (thin lines) for 850-hPa meridional wind (A) and precipitation (B). Units in (A) are ms^{-1} and units in (B) are mm day^{-1} .

Table 1. The 850-hPa wind rms error (ms^{-1}) for 3-day prediction.

	ECMWF	RPN	UKMO	NCEP	NRL	BMRC	JMA	Ensemble mean	Superensemble
Globe	4.1	4.7	5.8	5.8	4.2	4.7	4.8	4.0	3.5
Tropics	2.7	3.5	3.4	4.5	3.1	3.4	3.5	2.7	2.2
Monsoon	2.6	3.4	2.9	4.6	3.1	3.4	3.5	2.7	2.0
Europe	2.0	2.2	2.9	3.3	2.2	2.2	2.0	2.0	1.7
United States	2.6	3.1	3.8	4.5	2.9	3.0	3.1	2.9	2.5
Northern Hemisphere	3.0	3.7	3.8	4.8	3.2	3.6	3.9	3.3	2.8
Southern Hemisphere	4.8	5.4	7.2	6.6	5.0	5.5	5.6	4.6	4.2

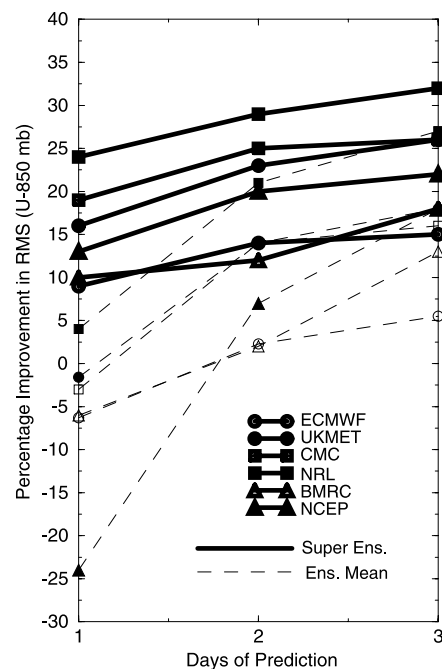


Fig. 2. Percentage improvement of rms error of selected models against the superensemble (solid line) and that of the ensemble mean (dashed line) for numerical weather prediction forecasts during August 1998.

timeline shows a persistent low rms error for the superensemble through about 20 months of integration (Fig. 1B). Because of the length of the forecast, the multimodel's skills were not expected to be high compared with monthly mean observed amounts. After 18 months of forecasts the superensemble retains a high degree of skill for all the dependent variables of the global models. This skill is beyond that of most current atmospheric general circulation models. These two timelines yield similar results for the superensemble. In contrast to the first timeline, all models used in the second timeline do not have identical initial conditions because of the systematic errors and biases of each model. These differences in the initial states do not contribute to any major differences in the overall performances of the multimodels, the ensemble mean, or the superensemble. In the second timeline, the models had already been integrated for 8 years. Thus, we attribute the results (Fig. 1B) to the robustness of the initial states of the ensemble in January 1987 and less so to the resilience of the statistical weights derived from the past (January 1979 through December 1986) behavior of the multimodels and prescribed SST and sea ice.

A number of weather services around the world use multilevel global models for daily numerical weather prediction. These models vary in their resolution, treatment of physics and dynamics, representation of orography, and initial data assimilation procedures. Collectively, they provide a useful multimodel data set. Thus, it is possible to explore the usefulness of the proposed multimodel superensemble for weather prediction. Using real-time data sets from the NCEP; ECMWF; Japan Meteorological Agency (JMA), Tokyo; BMRC; Research Provision Numerique (RPN), Montreal; and UKMO weather services, we examined the global data analyses and forecasts for June, July, and August 1998. These included the initial state and predictions through day 3 of the forecasts. The data sets for the first 61 days were designated as the control timeline. The

multimodel forecasts and the observed analysis for this period determined the statistical weights. These were handled separately for days 1, 2, and 3 of the multimodel forecasts. The results, averaged over August 1998, are shown for selected domains (5) in Table 1. The superensemble daily skill is similar to that obtained in the seasonal climate forecasts. The superensemble outperformed all other models, including the ensemble average. In the tropics and the monsoon region, errors were reduced by 25% over the ensemble average and skill increased up to 100% over some of the models. Errors are larger for the Southern than for the Northern Hemisphere. The tropical regions generally have a low predictability (as shown in the results from the models). Consequently, the improvements shown from the performance of the superensemble in the tropics and Asian monsoon domains are quite promising.

The superensemble also exhibits a higher skill compared with that of the ensemble mean for the entire global domain (Fig. 2). The evaluation of the skill relies on the observed (analysis) fields against which the respective forecasts are compared. That skill may be biased somewhat toward the group whose analysis is being used for the evaluation of skill. To avoid this bias, we verified the performance of the ensemble mean and the superensemble against each forecasting center's analyses. The superensemble's forecast skill of the 850-hPa meridional wind stands out regardless of the analysis used as a benchmark (Fig. 2).

There were 63 forecasts of tropical systems available from each of the multimodels during 1998 and there were 21 forecasts for 1997. These were provided from four diverse models: Florida State University (FSU), Tallahassee, model; Naval Oceanographic Global Predictions System (NOGAPS), Monterey, California, model; UKMO model; U.S. National Weather Service's GFDL model; and the official forecast from the National Hurricane Center. We applied the regression procedure by using the observed tracks (Table 2)

and maximum sustained winds (Table 3) for each of these storms, and we examined the multimodel forecasts every 12 hours for 3-day forecasts. We used the resulting statistics to assess the errors of the superensemble for this control period of 1998. The superensemble shows the smallest track errors compared with all other models. We also used a cross-validation procedure in which, successively, all but one of the storm's forecasts were included to evaluate the statistical weights. These forecast results are as robust as those of the test, illustrating the superior performance of the superensemble. The results from the ensemble averages are superior to all models except those of the superensemble. These results are better than current state-of-the-art methods for hurricane forecasting. Model changes are not desirable during the test and the forecast timelines (6). Any major model changes to the multimodels invalidate the use of this procedure. This limits the sources of available model data sets that can be used to test our scheme.

The superensemble described here is far superior, in terms of forecasts, to an ensemble mean. Six or seven models are needed to reduce the multimodel errors. Removing the bias of models (one at a time) and performing the ensemble mean of such (bias removed) multimodels are far less accurate than performing a collective bias removal as we have done.

Establishment of a multimodel superensemble forecast center for weather and seasonal climate forecasts would be a natural proposition from the outcome of these results. Given fast data communications by satellites and computers, it is possible for such a center to receive the multimodel forecasts from various global weather centers and to disseminate the superensemble forecasts back to the modelers and the user community in a timely manner.

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6. During the 2 years 1997 and 1998, three of these models—FSU, GFDL/NCEP, and NOGAPS—incorporated major changes; thus, we could not apply the statistics derived from 1998 to test the performance of the proposed method on the storms of 1997.
7. Supported by the following weather services and research institutions, to whom we are most indebted: AMIP, BMRC, CSIRO, ECMWF, FSU, GFDL, JMA, LMD, MPI, NCEP, NOGAPS, RPN, and UKMO. This research was supported by NASA grant NAG-1199, NASA grant NAG-4729, NOAA grant NA86GP0031, NOAA grant NA77WA0571, NSF grant ATM-9612894, and NSF grant ATM-9710336.

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Table 2. Hurricane track rms errors (degrees).

Model	NHC	NOGAPS	UKMO	GFDL	FSU	Ensemble average	Cross validation	Superensemble
Day 1	1.5	1.7	1.6	1.7	1.7	1.2	1.2	0.9
Day 2	2.8	3.4	2.6	3.0	3.4	2.4	1.9	1.5
Day 3	3.4	3.8	3.9	5.5	4.8	2.6	2.6	1.9

Table 3. Hurricane intensity forecast rms errors (ms⁻¹).

Model	NHC	GFDL	FSU	Ensemble average	Cross validation	Superensemble
Day 1	6.6	10.0	11.0	6.5	5.7	5.1
Day 2	9.9	10.3	11.7	8.8	9.0	7.7
Day 3	14.0	12.1	14.5	12.3	12.0	9.6