NEWS

The NBHM has set up a permanent Mathematics Olympiad Cell, which is functioning from the Department of Mathematics, Indian Institute of Science, Bangalore, and consists of some expert teachers, to oversee the Olympiad activity in India. The INMO is followed by a four-week training camp for the 30-odd toppers, starting sometime in May, organized by the MO Cell with the help of volunteers from around the country. So far, the training camp has been held either at the Indian Institute of Science, Bangalore, or at the Homi Bhabha Centre for Science Education, Mumbai. The MO Cell also produces written material useful for aspirants mathematical olympians. The efforts have paid good dividends. Since 1989 our teams have bagged a total of 5 gold, 27 silver and 21 bronze medals. Young people are turning up in greater numbers for various training programmes for the Olympiads.

India’s future at the IMO

The results of this year highlight also the importance of organized effort and training, rather than dependence on pure raw talent. For the first time in the ten years of our participation in the IMO, we had a very experienced team who had gone through three/two years of our training programme. The junior batch (the INMO-98 batch) which did not find a representative in the IMO team this year may perhaps have a lot to contribute next year; and we may also look forward to further achievements by Rishi Raj, who has one more chance (the other winners of this year have completed 12th standard or equivalent and will not be eligible for the content next year).

It also seems worthwhile to make the following observations: the cumulative experience has been that geometry is a strong point of Indian competitors; usually our team members come up with novel, off-beat solutions and sweep all the points for the geometry problems. On the other hand, combinatorics seems to be our bugbear and this is where we have to improve in order to better our performance in the IMO.

In terms of participation in the IMO, in addition to sending trained and talanted teams of students, we could also contribute questions. Finding a challenging problem (which nevertheless has a reasonable chance of being solved at least by the best young brains around!) is also a highly creative and difficult task. The problems proposed have to ‘compete’ with other proposals, in their merit as challenging and interesting problems. So far, in the ten years of our participation, three problems proposed by the training-faculty members were selected for the final contest; one each in 1990, 1992 and 1998.

While it is important to participate in the IMO movement and win laurels, it is certainly not to be viewed as an end in itself. A major need of our times is to enrich the mathematical culture, both in terms of research contributions of the highest level and to raise the general awareness and familiarity among a wide range of professionals, and young people with mathematical talent have a major role to play in this respect. The NBHM has followed this perspective and strives also to nurture the talent located through the Olympiad activity to achieve this objective, to the extent possible. The NBHM awards scholarships to about 30 leading students from each batch of the INMO if they choose to pursue mathematics for their undergraduate degree or if they enroll for a training programme in mathematics conducted by the NBHM, which can be undertaken concurrently to other regular courses that they may choose to join. The latter involves distance training during the working part of the academic year coupled with courses in the summer organized at some of the established centers of mathematics, for each batch. Over the years this has produced some fruitful results, which would however be premature to try and quantify.

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RESEARCH NEWS

A new model for promoting protein crystallization in solution

Biman Bagchi

Efficient crystallization of folded proteins from solutions is essential for three dimensional structure determination of the proteins. It is, however, not easy to grow large single crystals of proteins. In the absence of any microscopic understanding of protein crystallization, the growing of protein crystals has remained more of an art than science. In an article entitled ‘Crystallization of Macromolecules: General Principles’, Alexander McPherson wrote: ‘In principle, the crystallization of a protein, nucleic acid, or virus is little different than the crystallization of conventional small molecules. It requires the gradual creation of a supersaturated solution of the macromolecule and follows the spontaneous growth centres or nuclei’. Several recent studies, however, have questioned this age-old wisdom that crystallization of proteins is essentially the same as of small molecules and instead suggested that the kinetics of crystallization of proteins and colloids can indeed be very different from the crystallization of small molecules.

What are the factors that inhibit growth of single crystals? First, of course, is the fact that proteins tend to aggregate and precipitate if the conditions are not correct. This has formed a vicious cycle because we need high concentration of proteins so that the critical nucleus required to start crystal growth can form. Second, there is always the possibility that the formation of poly-crystals which can happen if multiple nucleation sites are present in the solution.

The way to facilitate the growth of
crystals is to find the conditions ideal for the formation of a 'stable' crystal nucleus. In ordinary crystallization where the size of the molecules is small, the nucleation can be understood in terms of the competition between the surface tension of the liquid–crystal interface and the relative stability of the crystalline phase over the liquid phase. The basic science of this problem is well-understood. One finds the following relation for the free energy of activation of the nucleus and for the size of the critical nucleus

$$\Delta G^* = 16\pi \rho^3 / 3 (\Delta G)^3,$$

(1)

$$r_c = 2\pi / \Delta G_c.$$  (2)

Here $\Delta G_c$ is the free energy difference per unit volume between the liquid and the solid, $\gamma$ is the surface tension. This is the classical picture of nucleation. This picture seems to be valid when the range of the attractive interaction is comparable to that of the molecular size, that is, molecular diameter, as in the Lennard-Jones potential between two Argon atoms. In Figure 1 a we show both the potential and the phase diagram of such a simple system, showing the gas, liquid, solid boundaries. The above mechanism appears to provide a satisfactory description of nucleation in atomic and molecular systems.

What is the difference between crystallization in molecular systems and in proteins and colloids? This is the question recently addressed to by several workers. According to ten Wolde and Frenkel, the main difference is the range of the attractive interaction. In molecular systems, this range is comparable to the size of the molecule itself. But in proteins and many colloids, this range is much smaller than the size of the molecule. A schematic description of such a potential is shown in Figure 1 b. Now, this much smaller range of potential can have a very interesting consequence. It is known that if the attractive potential is altogether absent, then the system cannot exist in the liquid phase and one considers only the gas–solid transition. When the range of the attractive interaction gradually decreases, one finds that the gas–liquid critical point gets depressed and eventually goes below the gas–solid coexistence. For some ranges of attractive potential, this critical point can be considered a metastable critical point. This phase diagram is shown in Figure 1 b. Now, what is really interesting is that the formation of a crystal nucleus can be greatly affected by the presence of this metastable critical point. The study of ten Wolde and Frenkel was motivated by the earlier studies of George and Wilson and of Rosenbaum et al. on the osmotic second virial coefficient of protein solutions. These authors have observed that the conditions under which a large number of globular proteins can be made to crystallize map into a narrow range of the osmotic second virial coefficient value. In addition, earlier studies on the phase diagram of uncharged, suspended colloids also suggested the scenario as noted by ten Wolde and Frenkel.

Classical nucleation occurs from high density and at low temperature when the crystalline phase is thermodynamically much more stable than the liquid phase. Solid differs from liquid on two counts. First is the order, second is the density. Thus, one can describe crystallization in terms of two-order parameters, $\rho$ for density and $m$ for the crystalline order. Theoretical studies indicate in the case of ordinary crystallization, micro-crystalline embryo is characterized more by the crystalline order than by the enhanced density—the latter remains essentially the same as in the liquid. Only after the growth has occurred to an appreciable extent does the density build up occur.

It was noted by ten Wolde and Frenkel that the situation changes drastically for proteins and colloids when the nucleation occurs at conditions near the metastable critical point. Because of the presence of large density fluctuations which can occur here without involving large activation energy, nucleation rate was found to be enhanced by several orders of magnitude. This was offered as the reason for anomalous enhancement in the protein crystallization rate observed in some cases.

Talanquer and Oxtoby analysed the reason for this result by using a theoretical formalism of statistical mechanics called the density functional theory. Conclusions from this study are essentially the same as those from simulations and can be summarized as follows. In the presence of a metastable critical point, the nucleation scenario can be totally different from what is observed for small molecules. The free energy of activation undergoes a sharp decrease near the metastable critical point. Here, the formation of the critical nucleus may be an aggregation process. The periodic order may appear later and play a much smaller role in the whole nucleation process. As already mentioned, for small molecules, exactly the opposite is expected.
Progress in interstellar chemistry

A key problem in modern astrophysics is the formation of galaxies. Considerable progress has been made on this problem in recent times, primarily because technological development has vastly enhanced the capabilities of astronomical instruments, giving us a glimpse into hitherto unseen eras in the history of the Universe.

The COBE-DMR mission, and several subsequent experiments, have successfully detected anisotropy in the cosmic microwave background on a range of angular scales; these have been interpreted as views of the extremely small fractional density inhomogeneities at an epoch when...